The Antitrust Prohibition of Excessive Pricing^{*}

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Abstract

Excessive pricing by a dominant firm is unlawful in many countries. To assess whether it is excessive, the dominant firm's price is often compared with price benchmarks. We examine the competitive implications of two such benchmarks: a retrospective benchmark where the price that prevails after a rival enters the market is used to assess whether the dominant firm's pre-entry price was excessive, and a contemporaneous benchmark, where the dominant firm's price is compared with the price that the firm charges contemporaneously in another market. We show that the two benchmarks restrain the dominant firm's behavior when it acts as a monopoly, but soften competition when the dominant firm compete with a rival. Moreover, a retrospective benchmark promotes entry, but may lead to inefficient entry.

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1 Introduction

Excessive pricing by a dominant firm is considered an unlawful abuse of dominant position in many countries. For example, Article 102 of the Treaty of the Functioning of the European Union prohibits a dominant firm from "directly or indirectly imposing unfair purchase or selling prices." Courts have interpreted this prohibition as including a prohibition of "excessive pricing."¹ A similar prohibition exists in many other countries, including all OECD countries, except the U.S., Canada, Australia, New Zealand, and Mexico.²

The antitrust prohibition of excessive pricing is highly controversial.³ Opponents claim that the prohibition may have a chilling effect on the incentive of firms to invest and that it creates considerable legal uncertainty due to the difficulty in determining whether prices are excessive. Moreover they claim that there is no need for antitrust intervention both because excessive pricing may attract competition and hence the problem is self-correcting, and also because the task of preventing dominant firms from charging high prices should be left to regulators who have the expertise and resources to set prices. They also point out that ex ante price regulation avoids the legal uncertainty associated with antitrust enforcement, which is backward looking and condemns excessive prices that were set in the past.⁴ On the other hand, proponents of the policy argue that many other antitrust rules also create uncertainty, that excessive pricing is not a self-correcting problem, and that price regulation is itself inefficient, so the antitrust prohibition of excessive pricing should be viewed as a complement to price regulations rather than a substitute.⁵

Part of the controversy surrounding the antitrust prohibition of excessive pricing stems from the fact that we still know very little about its competitive effects both in terms of theory as well in terms of empirical research. In fact, as far as we know, existing literature on the topic is all

¹Traditionally, courts have interpreted unfair prices as being low predatory prices. However, in the landmark *General Motors* case in 1975, the European Court of Justice held that a dominant firm's price is unfair if it is "excessive in relation to the economic value of the service provided." See Case 26/75, General Motors Continental v. Commission [1975] ECR 1367, at para. 12. The court did not clarify, however, what the "economic value of the service provided" is, or indeed, how to measure it. The court reiterated this position in the United Brands case in 1978 and held that "charging a price which is excessive because it has no reasonable relation to the economic value of the product supplied would be... an abuse." The court further held that "It is advisable therefore to ascertain whether the dominant undertaking has made use of the opportunities arising out of its dominant position in such a way as to reap trading benefits which it would not have reaped if there had been normal and sufficiently effective competition." Case 27/76, United Brands v. Commission [1978] ECR 207, at para. 249-250.

²See http://www.oecd.org/competition/abuse/49604207.pdf.

³For a recent overview of the debate, see Jenny (2017).

⁴See e.g., Evans and Padilla (2005), Motta and de Streel (2006, 2007), O'Donoghue and Padilla (2006), OECD (2011), and Gal and Nevo (2015, 2016).

⁵See e.g., Ezrachi and Gilo (2009) and Gilo (2018).

informal. The purpose of this paper is to contribute to the discussion by studying the competitive effects of the prohibition of excessive pricing in the context of a formal model. Although the model abstracts from many important real-life considerations, it does highlight two new effects, that to the best of our knowledge, were not mentioned earlier and may have important implications.

A main obstacles to an effective implementation of the prohibition of excessive pricing is the lack of a commonly agreed upon definition of what constitutes an "excessive price," or how to measure it. In practice, antitrust authorities and plaintiffs in excessive pricing cases often base their claims on a comparison of the dominant firm's price with some competitive benchmark, such as the firm's cost of production, or the firm's own price in other time periods, in different geographical markets, or in different market segments.⁶

In this paper, we consider two such price benchmarks. The first is a retrospective benchmark where the price that prevails after a rival enters the market is used to assess whether the dominant firm's pre-entry price was excessive. Retrospective benchmarks were used for example in class actions in Israel.⁷ In an early class action filed in 1998, the plaintiff alleged that the incumbent acquirer of Visa cards charged excessive merchant fees based on the fact that the fees dropped significantly following the entry of a new credit card company.⁸ In another case filed in 1997, the plaintiff alleged that prices for international phone calls charged by the former telecom monopoly Bezeq were excessive based on the fact that Bezeq lowered its prices by approximately 80% after the market was liberalized and two new rivals entered.^{9,10}

The second type of price benchmark that we study is a contemporaneous benchmark. Here,

⁶Motta and de Streel (2006) document various benchmarks used by the European Commission, including substantial differences between the dominant firm's prices across different geographic markets, or relative to the prices of smaller rivals. The OFT (2004) suggests similar benchmarks, including prices in other time periods, the prices of the same products in different markets, or the underlying costs when it is possible to measure them in an economically meaningful way.

⁷See Spiegel (2018) for an overview of these cases and for a broad overview of the antitrust treatment of excessive pricing in Israel.

⁸The class action was initially certified by the Tel Aviv District court, but was ultimately dismissed by the Israeli Supreme Court on appeal, mainly because the entrant went out of business shortly after entering the market, implying that the post-entry merchant fees were not a valid benchmark. See D.C.M. (T.A) 106462/98 Howard Rice v. Cartisei Ashrai Leisrael Ltd., P.M 2003(1) and Permission for Civil Appeal 2616/03 Isracard Ltd. v. Howard Rice, P.D. 59 (5) 701 [14.3.2005].

⁹Similarly to the Howard Rice case, this class action was also dismissed on appeal by the Israeli Supreme Court after being initially certified by the Tel Aviv District Court. The grounds for dismissal was that before liberalization, prices were set by regulators, meaning that Bezeq did not abuse its dominant position. See, D.C.A (T.A) 2298/01 Kav Machshava v. Bezeq Beinleumi Ltd. (Nevo, 25.12.2003) and See Permission for Civil Appeal 729/04 State of Israel et al., v. Kav Machshava et al., (Nevo, 26.4.2010).

¹⁰In another class action in Israel which is currently pending in court, the plaintiff alleges that Osem charged an excessive price for Israeli couscous (toasted pasta shaped like rice grains or little balls), based on the fact that following the entry of Sugat into the market in August 2013, Osem, which is the dominant firm in the market, lowered its price from 6.30 NIS to 4.99 in July 2015.

the dominant firm's price is compared with the price that the firm charges contemporaneously in another market. This type of benchmark was used for example by the European Court to determine that British Leyland charged an excessive price for certificates that left-hand drive vehicles conform to an approved type by comparing it to the price for certificates for right-hand drive vehicles.¹¹ Similarly, the OFT has determined that the price that Napp charged to community pharmacies in the UK for sustained release morphine was excessive by comparing it to the price charged to hospitals.¹²

A third type of price benchmark which is often used (but one that we do not consider in the current paper) is based on a price hike, typically after price controls are lifted. In a recent example, the British CMA imposed in December 2016 a £84.2 million fine on Pfizer and a £5.2 million fine on its distributor, Flynn Pharma, for charging an excessive price for phenytoin sodium capsules, which are used to treat epilepsy. The claim was based on a price hike of 2,300% - 2,600% following the de-branding of the drug, which meant that it was no longer subject to price regulation.¹³ Similarly, the Italian Market Competition Authority fined Aspen over €5 million in September 2016 for charging excessive prices for four anti-cancer drugs; Aspen raised their prices by 300% to 1,500% after acquiring the rights to commercialize them from GlaxoSmithKline.¹⁴

To study the competitive effects of a retrospective benchmark, we consider a two-period model, in which an incumbent, firm 1, is a monopoly in period 1, but may face competition in period 2 from an entrant, firm 2. Under a retrospective benchmark, firm 1 anticipates that if entry occurs in period 2 and its post-entry price drops, its pre-entry price may be deemed excessive. If it is, firm 1 pays a fine proportional to its excess revenue in period 1, which depends on the difference between its post-entry and its pre-entry prices. We then modify the model to consider a contemporaneous benchmark: instead of two periods, there are now two markets. Firm 1 is a

¹¹See British Leyland Public Ltd. Co. v. Commission [1986].

¹²See "Napp Pharmaceutical Holdings Limited And Subsidiaries (Napp)," Decision of the Director General of Fair Trading, No Ca98/2/2001, 30 March 2001.

¹³See https://www.gov.uk/government/news/cma-fines-pfizer-and-flynn-90-million-for-drug-price-hike-to-nhs. After patents expired in September 2012, Pfizer sold the rights for distributing the drug in the UK to Flynn Pharma, which in turn de-branded it (to avoid price regulation), and raised its price to the British National Health Services from $\pounds 2.83$ to $\pounds 67.50$, before reducing it to $\pounds 54$ in May 2014.

¹⁴See https://www.natlawreview.com/article/italy-s-agcm-market-competition-authority-fines-aspen-eur-5million-excessive The European Commission recently announced that it is opening an investigation against Aspen for excessive pricing of the drugs outside of Italy. See http://europa.eu/rapid/press-release_IP-17-1323_en.htm. Another recent example is a class action in Israel alleging that Dead Sea Works Ltd, which is a monopoly in the supply of potash, charged farmers an excessive price for potash. The Central District Court approved a settlement partly on the grounds that Dead Sea Works raised its price from \$200 per ton in 2007 to \$1,000 per ton in 2008-9, after it allegedly joined an international potash cartel. See Class Action (Central District Court) 41838-09-14 Weinstein v. Dead Sea Works, Inc. (Nevo, 29.1.2017).

monopoly in market 1, but faces competition from firm 2 in market 2. Firm 1's price in market 1 may be deemed excessive if it exceeds the price of firm 1 in market 2.

Our analysis has a number of interesting implications. First, the prohibition of excessive pricing involves a tradeoff: it restraints firm 1's behavior when it acts as a monopoly (the pre-entry period under a retrospective benchmark and market 1 under a contemporaneous benchmark), but induces it to be softer when it competes with firm 2. The reason is that a smaller gap between the price that firm 1 charges as a monopoly and under competition, means a smaller excessive revenue and hence a smaller fine. The softer behavior of firm 1 under competition induces firm 2 to be more aggressive if the two firms compete by setting quantities but be softer if they compete by setting prices. From the point of view of consumers, the prohibition of excessive pricing leads to lower prices when firm 1 is a monopoly, but higher prices in the benchmark market where firms 1 and 2 compete.

Second, the prohibition of excessive pricing may completely deter excessive pricing by firm 1. In a quantity-setting model with homogeneous products, this occurs when firm 1 sets its output such that its resulting prices are equal over time (under a retrospective benchmark) or across markets (contemporaneous benchmark). The incentive to ensure that prices are equal is especially strong when the expected fine that firm 1 pays when its price as a monopoly is deemed excessive is high (under both benchmarks) and also when the discounted probability of entry in period 2 is large (under a retrospective benchmark). In a price-setting model with symmetric costs, a retrospective benchmark induces firm 1 to set its post-entry price above the entrant's price. Hence firm 1 makes no sales when firm 2 enters and hence there is no observed post-entry transaction price for firm 1 and therefore no benchmark to assess its pre-entry price.

Third, we show that in a quantity-setting model with homogenous products and a linear demand function, the lower pre-entry price that emerges in equilibrium benefits consumers more than the higher post-entry price hurts them. Consequently, consumers are overall better-off when a retrospective benchmark is used to assess whether the pre-entry price was excessive. By contrast, in a price-setting model with symmetric costs, a retrospective benchmark allows the entrant, firm 2, which monopolizes the market in period 2, to charge a price which exceeds the counterfactual price that would have prevailed without a retrospective benchmark. And, since firm 1 makes no sales in period 2 and hence its period 1 price cannot be deemed excessive, firm 1 charges the monopoly price in period 1. Consequently, the retrospective benchmark harms consumers in period 2 without benefitting them in period 1.

Fourth, firm 1 has a stronger incentive to ensures that its pre-entry price is low when the discounted probability of entry high. Consequently, a retrospective benchmark benefits consumers especially when the probability of entry is high. This result is interesting because it is often argued that there is no need to intervene in excessive pricing cases when the probability of entry is high, since then the "market will correct itself."¹⁵ This argument, however, merely points out that the harm to consumers prior to entry is going to be short lived and ignores ignores the fact that a retrospective benchmark to assess excessive pricing can alleviates this harm, especially when the probability of entry is high.

Fifth, a retrospective benchmark makes firm 1 softer once entry occurs and hence promotes entry. This result stands in sharp contrast to the often made claims that the prohibition of excessive pricing discourages entry by inducing the incumbent to lower its price.¹⁶ Although in our model the incumbent charges a lower price prior to entry, what matters for the entrant is not the pre-entry behavior of the incumbent but rather its post-entry behavior. And, as we show, a retrospective benchmark induces the incumbent to be softer following entry in order to ensure that its post-entry price does not fall by too much below its pre-entry price.

As far as we know, our paper is the first to examine the competitive implications of the prohibition of excessive prices in the context of a formal economic model. Existing literature on excessive prices is all based on informal legal policy discussion. Evans and Padilla (2005), Motta and de Streel (2006, 2007), O'Donoghue and Padilla (2006), and Green (2006) critically examine the case law and policy issues, consider different possible benchmarks that can be used to assess if prices are excessive, and discuss their potential drawbacks. Gal (2004) compares the EU and U.S. antitrust laws that apply to the prohibition of excessive pricing and explains the difference between the two systems. Ezrachi and Gilo (2010a, 2010b) critically discuss the main grounds for the reluctance of some antitrust agencies and courts to intervene in excessive pricing cases, while Ezrachi and Gilo (2009) discuss the retrospective benchmark that we also consider in this paper,

¹⁵For instance, the OECD competition committee (OECD, 2011) emphasizes that "The existence of high and nontransitory structural entry barriers are probably considered the most important single requirement for conducting an excessive price case." It also adds that "This requirement is based on the fundamental proposition that competition authorities should not intervene in markets where it is likely that normal competitive forces over time eliminate the possibilities of a dominant company to charge high prices." Likewise, O'Donoghue and Padilla (2006) write that "The key consideration is to limit intervention to cases in which entry barriers are very high and, therefore, where there is a reasonable prospect that consumers could be exploited" (p. 635–636). Similraly, Motta and de Streel (2006) write that "exploitative practices are self-correcting because excessive prices will attract new entrants" (p. 15).

¹⁶For instance, Areeda and Hovenkamp (2001) write: "While permitting the monopolist to charge its profitmaximizing price encourages new competition, forcing it to price at a judicially administered 'competitive' level would discourage entry and thus prolong the period of such pricing" (para. 720b). Similar arguments appear in Whish (2003, p. 688–689) and in Economic Advisory Group on Competition Policy (2005, p. 11).

but do it in the context of a legal policy paper, without a formal model.

Our analysis is related to the literature on most-favoured-customer (MFN) clauses, which guarantee past consumers a rebate if the price falls. Cooper (1986), Neilson and Winter (1993), and Schnitzer (1994) show that competing firms have an incentive to adopt retroactive MFN's in order to facilitate collusion (MFN's make firms reluctant to cut future prices in order to avoid paying rebates to past consumers). Although the fine that the dominant firm may have to pay when the post-entry price falls is akin to a rebate to past consumers, the dominant firm is much better off without it, since then it is free to exploit its monopoly power prior to entry, and can respond optimally to entry if it occurs. Moreover, while MFN's facilitate collusion, the prohibition of excessive pricing may be pro-competitive.

A retrospective benchmark for assessing whether the incumbent's pre-entry price is excessive is reminiscent of the legal rules proposed by Williamson (1977), Baumol (1979), and Edlin (2002), to deter predatory pricing. These rules are also based on the response of a dominant firm to entry.¹⁷ However unlike these papers, we do not propose a new legal rule, but rather examine the competitive implications of existing price benchmarks that are used in practice and are likely to become even more popular, especially in private antitrust enforcement.

The rest of the paper is organized as follows: Section 2 studies the competitive implications of a retrospective benchmark under quantity competition, and Section 3 studies its competitive implications under price competition. Section 4 studies the competitive implications of a contemporaneous benchmark under quantity and price competition. We conclude in Section 5. The Appendix contains technical proofs.

2 A retrospective benchmark under quantity competition

We begin by studying the competitive effects of a retrospective benchmark for assessing whether the price of a dominant firm is excessive under the assumption that firms produce homogenous products and compete by setting quantities. The assumption that products are homogenous is a reasonable approximation for the two Israeli class actions mentioned in the Introduction, as well as

¹⁷Williamson (1977) proposes that following entry, the dominant firm will not be able to raise output above the pre-entry level for 12 - 18 months. Edlin (2002) proposes to block a dominant firm from significantly cutting its price for a period of 12 - 18 months following entry. Both rules prevent predation. Baumol (1979) proposes that the incumbent will not be allowed to raise its price if and when the entrant exits the market, unless this is justified by cost or demand changes. This rule prevents recoupement. Edlin et al (2016) provide experimental evidence that both the Edlin and Baumol rules significantly improve consumer welfare when subjects are experienced.

several other class actions that are currently pending in court.¹⁸

There are two time periods. In period 1, firm 1 operates as a monopoly. In period 2 firm 1 continues to operate as a monopoly with probability $1 - \alpha$, but faces competition from firm 2 with probability α . We assume that firms 1 and 2 produce homogenous products, and compete by setting quantities. For simplicity, we assume that both firms have the same constant marginal cost c and denote the (downward sloping) inverse demand function by p(Q), where Q is the aggregate output level. To ensure that the market is viable, we assume that p(0) > c. The intertemporal discount factor is δ .

The prohibition of excessive pricing is enforced in period 2 as follows: if entry occurs and the period 2 price, p_2 , falls below the period 1 price, p_1 , a court rules that p_1 was excessive with probability γ . The parameter γ reflects various legal factors, including the stringency of antitrust enforcement against excessive pricing, the availability of data on prices and quantities needed to support the case, and potential defenses that the dominant firm may have for its high prices, such as the need to recoup large investments. When p_1 is deemed excessive, firm 1 has to pay a fine in proportion to its excess revenue in period 1; the fine is given by $\tau (p_1 - p_2) Q_1$, where $\tau > 0$, and Q_1 is firm 1's output in period 1, and $p_1 - p_2$ is the per-unit excess revenue. To ensure that we have interior solutions, we will make the following assumptions:

A1
$$p'(Q) + p''(Q)(1 + \gamma \tau)Q < 0$$

A2
$$\gamma \tau < 1$$

Assumption A1 is a modified version of the standard assumption that p'(Q) + p''(Q)Q < 0. It is stronger because $\gamma \tau > 0$, but like the standard assumption, it also holds when the demand function is concave or not too convex. The assumption ensures that the marginal revenue functions are downward sloping. Assumption A2 ensures that the expected fine that firm 1 pays is not so large that firm 1 wishes to exit in period 2 when firm 2 enters.¹⁹

In the next two sections we characterize the equilibrium in our model. We begin in Section 2.1 by considering the equilibrium in period 2, and then we turn to period 1 in Section 2.2.

¹⁸Currently, there are 22 pending class action law suits in Israel alleging excessive pricing (see Spiegel 2018 for detail). Among the products involved in these cases, are natural gas, white cheese, yellow cheese, heavy cream, cocoa powder, margarine, and green tea. Arguably, these products are fairly homogenuous.

¹⁹For example, in the Israeli cases mentioned in the Introduction, τ was equal to 1 as plaintiffs were suing for the actual damages. Since $\gamma < 1$, $\gamma \tau$ was indeed below 1.

2.1 The equilibrium in period 2

Absent entry in period 2, the court cannot evaluate whether p_1 was excessive. Hence, firm 1 simply maximizes its period 2 profit by producing the monopoly output, Q^M , defined implicitly by $MR(Q) \equiv p(Q) + p'(Q)Q = c ("M" stands for "Monopoly").^{20}$

Now suppose that firm 2 enters in period 2 and let q_1 and q_2 be the resulting output levels. Given firm 1's output in period 1, Q_1 , firm 1 can be found liable for having charged an excessive price in period 1 if and only if $q_1 + q_2 > Q_1$ (output in period 2 exceeds firm 1's output in period 1) because then $p(q_1 + q_2) < p(Q_1)$. Recalling that firm 1 is found liable with probability γ and the fine it pays in this case is equal to $\tau (p_1 - p_2) Q_1$, where $p_1 = p(Q_1)$ and $p_2 = p(q_1 + q_2)$, the period 2 profits of firms 1 and 2 are given by

$$\pi_1(q_1, q_2) = \begin{cases} (p(q_1 + q_2) - c)q_1, & q_1 + q_2 \le Q_1, \\ (p(q_1 + q_2) - c)q_1 - \gamma\tau [p(Q_1) - p(q_1 + q_2)]Q_1, & q_1 + q_2 > Q_1. \end{cases}$$

and

$$\pi_2(q_1, q_2) = (p(q_1 + q_2) - c)q_2.$$

The next result characterizes the best-response functions of the two firms in period 2.

Lemma 1: (The best-response functions under entry) Suppose that firm 2 enters in period 2. Then, firm 2's best-response function is given by $BR_2(q_1) = r_2^C(q_1)$. Given Assumption A1, firm 1's best-response function is given by

$$BR_{1}(q_{2}) = \begin{cases} r_{1}^{C}(q_{2}), & p(Q_{1}) + p'(Q_{1})(Q_{1} - q_{2}) < c, \\ Q_{1} - q_{2}, & p(Q_{1}) + p'(Q_{1})(Q_{1} - q_{2}) > c > p(Q_{1}) + p'(Q_{1})((1 + \gamma\tau)Q_{1} - q_{2}), \\ r_{1}^{E}(q_{2}), & p(Q_{1}) + p'(Q_{1})((1 + \gamma\tau)Q_{1} - q_{2}) > c, \end{cases}$$

where $r_i^C(q_j)$ is the "Cournot" best-response function ("C" stands for "Cournot"), defined implicitly by

$$p(q_i + q_j) + p'(q_i + q_j)q_i = c,$$
(1)

²⁰Note that if $Q_1 > Q^M$, the price in period 2, p_2 , exceeds the price in period 1, p_1 and in principle may be deemed excessive. However, absent entry, there is no change in market structure and hence no competitive benchmark in either period, so it is hard to make the case that p_2 is excessive. Although in the Introduction we mentioned a few cases where prices were deemed excessive due to price hikes without entry or exit, the price hikes followed the removal of price controls (Pfizer), a sale of the distribution rights to a new distributor (Pfizer and Aspen), or alleged cartelization (Dead Sea Works).

and $r_1^E(q_2)$ is firm 1's best-response function against q_2 when p_1 is excessive ("E" stands for "Excessive"), defined implicitly by

$$p(q_1 + q_2) + p'(q_1 + q_2)(q_1 + \gamma \tau Q_1) = c.$$
(2)

Assumption A1 ensures that both best-response functions are downward sloping in the (q_1, q_2) space and $BR'_1(\cdot) \leq -1 \leq BR'_2(\cdot) < 0$, with $BR'_1(\cdot) = -1$ only when $q_1 + q_2 = Q_1$.

Proof: See the Appendix.

The best-response function of firm 1 is illustrated in Figure 1.²¹ The figure shows the Cournot best-response function of firm 1, $r_1^C(q_2)$, as well as its best-response function when $p_1 > p_2$, $r_1^E(q_2)$. The latter lies everywhere below $r_1^C(q_2)$ because when $p_1 > p_2$, firm 1 has, in expectation, an extra marginal cost. This cost arises because an increase in q_1 lowers p_2 and therefore increases the excessive revenue, $[p(Q_1) - p(q_1 + q_2)]Q_1$, on which firm 1 pays a fine if found liable in court. When $q_1 + q_2 = Q_1$ lies above $r_1^C(q_2)$, the aggregate output in period 2, $r_1^C(q_2) + q_2$, falls short of the output in period 1, Q_1 , so $p_2 > p_1$, meaning that p_1 is not excessive. Hence, the best-response of firm 1 is given by $r_1^C(q_2)$. By contrast, when $q_1 + q_2 = Q_1$ lies below $r_1^E(q_2)$, the aggregate output in period 2, $r_1^E(q_2)$, the aggregate output in period 2, $r_1^E(q_2)$, and, when $q_1 + q_2 = Q_1$ lies below $r_1^C(q_2)$ but above $r_1^E(q_2)$, firm 1 sets q_1 such that $q_1 + q_2 = Q_1$ to ensure that $p_1 = p_2$. Note that in this case, p_1 is not excessive, but firm 1 cannot play its Cournot best response against q_2 because then p_1 will be deemed excessive. In other words, firm 1 is constrained in this case to keep q_1 below the $q_1 + q_2 = Q_1$ line to ensure that p_1 is not retrospectively deemed excessive.

Overall then, the best-response function of firm 1 is given by the thick downward sloping line in Figure 1. The figure shows three different cases, depending on how large Q_1 is.

²¹The best-response functions in Figures 1 and 2 are drawn as linear only for convinience; in general they need not be linear. It the following analysis, however, we do not rely on the linearity of the best-response functions.



Figure 1: The best-response function of firm 1 in period 2

We denote the Nash equilibrium in period 2 following entry by (q_1^*, q_2^*) and prove the following result:

Lemma 2: (Both firms are active in the market when firm 2 enters) $q_1^* > 0$ and $q_2^* > 0$.

Proof: See the Appendix.

Given Lemma 2, three types of equilibria can emerge, depending on how high Q_1 is. We illustrate the three equilibria in Figure 2.



Figure 2: the Nash equilibrium in period 2

The first type of equilibrium, illustrated in Figure 2a, is the Cournot equilibrium, (q_1^C, q_2^C) . It is attained when Q_1 exceeds the aggregate Cournot output in period 2. Then, p_1 is not excessive, so the best-response function of firm 1 is indeed given by the Cournot best-response function, $r_1^C(q_2)$. Since the Cournot best-response functions are symmetric, the Cournot equilibrium lies on the diagonal in the (q_1, q_2) space.

The second type of equilibrium emerges when Q_1 is below the aggregate Cournot output, but above the aggregate output when p_1 is excessive (the latter is attained at the intersection of $r_1^E(q_2)$ and $r_2^C(q_1)$). As Figure 2b illustrates, firm 1 sets in this case $q_1 = Q_1 - q_2$, to ensure that $p_1 = p_2$, so p_1 is not excessive. The equilibrium then, (q_1^*, q_2^*) , is defined by the intersection of $q_1 + q_2 = Q_1$ with $r_2^C(q_1)$. Since $q_1 + q_2 = Q_1$ passes below the Cournot equilibrium point, (q_1^C, q_2^C) , the equilibrium point (q_1^*, q_2^*) lies above the diagonal in the (q_1, q_2) space, meaning that $q_2^* > q_1^*$.

The third equilibrium, illustrated in Figure 2c, arises when Q_1 is even lower than the aggregate output produced when $r_1^E(q_2)$ and $r_2^C(q_1)$ intersect. Now firm 1 plays a best response against q_2 , despite the fact that the resulting price renders p_1 excessive. The equilibrium is then defined by the intersection of $r_1^E(q_2)$ and $r_1^C(q_1)$. Since $r_1^E(q_2) < r_1^C(q_1)$, the equilibrium point again lies above the diagonal in the (q_1, q_2) space, so once again, $q_2^* > q_1^*$.

In Lemma 6 below, we prove that in equilibrium, $Q_1 \leq q_1^C + q_2^C$, meaning that the situation illustrated in Figure 2a cannot be an equilibrium. Noting that in Figures 2b and 2c, firm 1's bestresponse function lies below its Cournot best-response function, the Nash equilibrium in period 2 is attained in the (q_1, q_2) space below a 45⁰ line that passes through $q_1^C + q_2^C$. Consequently, $q_1^* + q_2^* \leq q_1^C + q_2^C$, with equality holding only when $\gamma \tau = 0$, in which case $r_1^E(q_2) = r_1^C(q_1)$.

We summarize the discussion in the next Lemma.

Lemma 3: (The equilibrium in period 2 under entry) The equilibrium in period 2 when firm 2 enters, (q_1^*, q_2^*) , is defined implicitly by the intersection of $r_1^E(q_2)$ and $r_2^C(q_1)$ if p_1 is excessive, and by the intersection of $q_1+q_2 = Q_1$ and $r_2^C(q_1)$ if p_1 is not excessive. Either way, $q_1^* \leq q_1^C = q_2^C \leq q_2^*$ and $q_1^* + q_2^* \leq q_1^C + q_2^C$, with equalities holding only when $\gamma \tau = 0$.

Lemma 3 implies that when firm 2 enters in period 2, the period 1 output level, Q_1 , matters: either p_1 is excessive and firm 1 pays in expectation a fine that depends on Q_1 , or firm 1 chooses its output in period 2 such that $q_1 + q_2 = Q_1$ to ensure that p_1 is not excessive. Either way, in equilibrium, q_1 and q_2 depend on Q_1 .

An important implication of Lemma 3 is that whenever $\gamma \tau > 0$, $\pi_2(q_1^*, q_2^*) > \pi_2(q_1^*, q_2^C) > \pi_2(q_1^*, q_2^C)$

 $\pi_2 (q_1^C, q_2^C)$, where the first inequality follows by revealed preferences and the second follows because $q_1^* < q_1^C$. Hence, the prohibition of excessive pricing boosts the profit of firm 2 and therefore encourages entry, contrary to what many scholars claim. As we mention in the Introduction, the claims that the prohibition of excessive pricing discourages entry is based on the idea that a high pre-entry price attracts entry, while a low pre-entry price may discourage it. However, entrants base their entry decisions on the anticipated behavior of incumbents after entry takes place, not before it does. As the analysis above shows, the fine that firm 1 may have to pay in period 2 softens the behavior of firm 1 in period 2 and therefore encourages entry.

Whether the equilibrium in period 2 is such that p_1 is excessive (as in Figure 2c) or is not excessive (as in Figure 2b) depends on the size of Q_1 . Let \overline{Q}_1 be the critical value of Q_1 such that p_1 is excessive if $Q_1 < \overline{Q}_1$ and is not excessive if $Q_1 \ge \overline{Q}_1$. Note that \overline{Q}_1 is attained when $q_1 + q_2 = Q_1$ passes through the intersection of $r_1^E(q_2)$ and $r_2^C(q_1)$. Hence, \overline{Q}_1 satisfies (1) when $q_i = q_2$, (2), and $q_1 + q_2 = \overline{Q}_1$. Substituting for q_2 from the last equation into (1) and (2), adding the two equations and simplifying, \overline{Q}_1 is implicitly defined by the equation

$$p\left(\overline{Q}_{1}\right) + \left(\frac{1+\gamma\tau}{2}\right)p'\left(\overline{Q}_{1}\right)\overline{Q}_{1} = c.$$
(3)

Lemma 4: (The properties of \overline{Q}_1) $Q^M < \overline{Q}_1 < q_1^C + q_2^C$ and \overline{Q}_1 is decreasing with the size of the expected fine, $\gamma \tau$.

Proof: See the Appendix.

Lemma 4 provides a lower and upper bound on \overline{Q}_1 , which is the critical value of Q_1 that delineates equilibria in which p_1 is excessive from equilibria in which p_1 is not excessive. Recalling that p_1 is excessive only when $Q_1 < \overline{Q}_1$, the second part of Lemma 4 implies that as the expected fine, $\gamma \tau$, increases, firm 1 is more likely to set Q_1 such that p_1 will not end up being excessive. In the limit, as $\gamma \tau$ approaches 1, (3) coincides with the first-order condition for Q^M , implying that $\overline{Q}_1 = Q^M$. Since in Lemma 7 below we prove that $Q_1 > Q^M$, it follows that as $\gamma \tau$ approaches 1, $Q_1 > Q^M = \overline{Q}_1$, implying that p_1 is never deemed excessive in period 2.

We conclude this section by studying the effect of Q_1 on the equilibrium in period 2.

Lemma 5: (The effect of Q_1 on the equilibrium in period 2) Suppose that $Q_1 < \overline{Q}_1$ (p_1 is excessive); then $-\gamma\tau < \frac{\partial q_1^*}{\partial Q_1} < 0 < \frac{\partial q_2^*}{\partial Q_1} < \gamma\tau$ and $-\gamma\tau < \frac{\partial (q_1^*+q_2^*)}{\partial Q_1} < 0$. If $Q_1 \ge \overline{Q}_1$ (p_1 is not excessive), then $\frac{\partial q_1^*}{\partial Q_1} > 1$, $\frac{\partial q_2^*}{\partial Q_1} < 0$, and $\frac{\partial (q_1^*+q_2^*)}{\partial Q_1} = 1$.

Proof: See the Appendix.

Lemma 5 shows that Q_1 has a non-monotonic effect of the equilibrium output levels in period 2: q_1^* is decreasing with Q_1 when $Q_1 < \overline{Q}_1$, and increasing with Q_1 when $Q_1 \ge \overline{Q}_1$, and conversely for q_2^* . Intuitively, whenever $Q_1 < \overline{Q}_1$, p_1 is excessive, so firm 1 has an incentive to cut q_1^* in order to keep p_2 high, and thereby lower the expected fine it has to pay. This incentive becomes stronger as Q_1 increases because the fine is proportional to Q_1 . However, once $Q_1 \ge \overline{Q}_1$, firm 1 chooses q_1^* such that $q_1^* + q_2^* = Q_1$, so now an increase in Q_1 allows firm 1 to expand q_1^* . Since q_2^* and q_1^* are strategic substitutes, Q_1 has the opposite effect on q_2^* .

2.2 The equilibrium in period 1

Firm 1 chooses Q_1 in period 1 to maximize the discounted sum of its period 1 and period 2 profits:

$$\Pi_1(Q_1) = (p(Q_1) - c)Q_1 + \delta \left[(1 - \alpha) \pi^M + \alpha \pi_1(q_1^*, q_2^*) \right],$$

where $(p(Q_1) - c)Q_1$ is firm 1's profit in period 1, $\pi^M \equiv \pi_1(q_1^M, 0)$ is firm 1's monopoly profit in period 2 absent entry, $\pi_1(q_1^*, q_2^*)$ is firm 1's profit in period 2 when entry occurs, and δ is the intertemporal discount factor.

Before proceeding, it is worth noting that in equilibrium in must be that $Q_1 \ge Q^M$, otherwise firm 1 can raise Q_1 slightly towards Q^M and make more money in period 1, while lowering p_1 and hence making it less likely to be deemed excessive in period 2. Moreover, it must be that $Q_1 \le q_1^C + q_2^C$, otherwise firm 1 can raise its profit in period 1 by lowering Q_1 slightly towards $q_1^C + q_2^C$, without rendering p_1 excessive (recall that the aggregate output in period 2 can be at most equal to the aggregate Cournot level, $q_1^C + q_2^C$). Hence,

Lemma 6: (A bound on Q_1) The period 1 output of firm 1, Q_1 , is between the monopoly output and the aggregate Cournot output: $Q^M \leq Q_1 \leq q_1^C + q_2^C$.

Since $Q_1 \leq q_1^C + q_2^C$, the equilibrium is attained in the (q_1, q_2) space on the $q_1 + q_2 = Q_1$ line (as in Figure 1b) or below it (as in Figure 1c). The discounted expected profit of firm 1 can be rewritten as:

$$\Pi_{1}(Q_{1}) = \begin{cases}
(p(Q_{1}) - c)Q_{1} + \delta(1 - \alpha) \pi^{M} & Q^{M} \leq Q_{1} < \overline{Q}_{1}, \\
+\delta\alpha \left[(p(q_{1}^{*} + q_{2}^{*}) - c)q_{1}^{*} - \gamma\tau (p(Q_{1}) - p(q_{1}^{*} + q_{2}^{*})) Q_{1} \right], & (4) \\
(p(Q_{1}) - c)Q_{1} + \delta(1 - \alpha) \pi^{M} + \delta\alpha (p(Q_{1}) - c) q_{1}^{*}, & Q_{1} \geq \overline{Q}_{1},
\end{cases}$$

where (q_1^*, q_2^*) is defined by the intersection of $r_1^E(q_2)$ and $r_2^C(q_1)$ if $Q_1 < \overline{Q}_1$ and by the intersection of $q_1 + q_2 = \overline{Q}_1$ and $r_2^C(q_1)$ if $\overline{Q}_1 \leq Q_1 \leq q_1^C + q_2^C$. Note that at $\overline{Q}_1, q_1^* + q_2^* = \overline{Q}_1$, so $p(\overline{Q}_1) = p(q_1^* + q_2^*)$. Moreover, recalling that \overline{Q}_1 is attained when $q_1 + q_2 = Q_1$ passes through the intersection of $r_1^E(q_2)$ and $r_2^C(q_1)$, it follows that at \overline{Q}_1, q_1^* and q_2^* are equal at the first and second lines of (4); hence, $\Pi_1(Q_1)$ is continuous at $Q_1 = \overline{Q}_1$.

Let Q_1^* denote the optimal choice of Q_1 . In order to characterize Q_1^* , we shall make the following assumption:

A3 $\Pi_1(Q_1)$ is piecewise concave (i.e., concave in each of its two relevant segments)

In the next section, we show that when the demand function is linear, Assumption A3 holds provided that the discounted probability of entry in period 2, $\delta \alpha$, is below 0.9. Indeed, it is easy to see that when $\alpha = 0$, $\Pi_1(Q_1)$ is concave by Assumption A1; by continuity this is also true so long as α is not too large. Given Assumption A3, we now characterize the equilibrium choice of Q_1 .

Lemma 7: (The choice of Q_1^*) $Q_1^* > Q^M$. Let $\frac{\partial q_1^*}{\partial Q_1^+}$ be the derivative of q_1^* with respect to Q_1 when $Q_1 \ge \overline{Q}_1$ (p_1 is not excessive) and $\frac{\partial q_2^*}{\partial Q_1^-}$ the derivative of q_2^* with respect to Q_1 when $Q_1 < \overline{Q}_1$ (p_1 is excessive). Then,

- (i) $Q_1^* < \overline{Q}_1$, implying that p_1 ends up being excessive if $\frac{\partial q_1^*}{\partial Q_1^+} < \frac{(1+\delta\alpha)(1-\gamma\tau)}{\delta\alpha(1+\gamma\tau)}$ and $\frac{\partial q_2^*}{\partial Q_1^-} > \frac{\gamma\tau(1+2\delta\alpha)-1}{\delta\alpha(1+\gamma\tau)}$. Both inequalities hold when $\delta\alpha$ is sufficiently small. Moreover, $\delta\alpha < \frac{1-\gamma\tau}{2\gamma\tau}$ is necessary for the first inequality and sufficient for the second.
- (ii) $Q_1^* > \overline{Q}_1$, implying that p_1 does not end up being excessive if $\frac{\partial q_1^*}{\partial Q_1^+} \ge \frac{(1+\delta\alpha)(1-\gamma\tau)}{\delta\alpha(1+\gamma\tau)}$, and $\frac{\partial q_2^*}{\partial Q_1^-} > \frac{\gamma\tau(1+2\delta\alpha)-1}{\delta\alpha(1+\gamma\tau)}$. $\delta\alpha > \frac{1-\gamma\tau}{2\gamma\tau}$ is sufficient for the first inequality and necessary for the second inequality.

(iii) Firm 1's problem has two local optima, one below and one above \overline{Q}_1 if $\frac{\partial q_1^*}{\partial Q_1^+} > \frac{(1+\delta\alpha)(1-\gamma\tau)}{\delta\alpha(1+\gamma\tau)}$, and $\frac{\partial q_2^*}{\partial Q_1^-} < \frac{\gamma\tau(1+2\delta\alpha)-1}{\delta\alpha(1+\gamma\tau)}$, where $\delta\alpha > \frac{1-\gamma\tau}{2\gamma\tau}$ is sufficient for both inequalities.

Proof: See the Appendix.

To understand Lemma 7 note that when $Q_1 = Q^M$, firm 1 maximizes its profit in period 1, but then if entry takes place in period 2, the aggregate output in period 2 exceeds Q^M , so p_1 is rendered excessive and firm 1 may have to pay a fine (by Lemma 4, $Q^M < \overline{Q}_1$, so at $Q_1 = Q^M$, p_1 is excessive). Raising Q_1 slightly above Q^M entails a second-order loss of profits in period 1, but leads to a first-order reduction of the expected fine that firm 1 pays in period 2. Hence, firm 1 sets Q_1 above Q^M , implying that the prohibition of excessive pricing has a pro-competitive effect on the pre-entry behavior of firm 1, even if eventually, firm 1 is not found liable in period 2.

A further increase in Q_1 involves a trade-off: firm 1 loses money in period 1 as it expands Q_1 above the monopoly level, but it relaxes the constraint that firm 1 faces in period 2 and allows it to expand its period 2 output without increasing the fine it may pay should p_1 be deemed excessive. Once $Q_1 \ge \overline{Q}_1$, firm 1 ensures that p_1 will not be deemed excessive by setting q_1^* in period 2 such that $q_1 + q_2 = Q_1$, to ensure that $p_1 = p_2$. Lemma 7 shows that when firm 1 expands Q_1 to the point where p_1 is no longer excessive, it actually expands it beyond \overline{Q}_1 , despite the fact that the expansion entails a loss of profit in period 1 (as Q_1 moves further away above Q^M). The reason why firm 1 expands Q_1 is that doing so allows it to raise q_1 closer to its Cournot best-response function in period 2 without rendering p_1 excessive.

Lemma 7 shows that, so long as $\delta \alpha$, which represents the discounted probability of entry, is not too large, firm 1 sets $Q_1 < \overline{Q}_1$, in which case p_1 is excessive. Firm 1 then still expands Q_1 above Q^M to relax the constraint on its period 2 output, but does not expand it all the way to the point where p_1 is no longer excessive. By contrast, when $\delta \alpha$ is large relative to $\frac{1-\gamma\tau}{2\gamma\tau}$, firm 1 may raise Q_1 beyond \overline{Q}_1 to ensure that p_1 is not excessive. Note though that when $\gamma \tau < \frac{1}{3}, \frac{1-\gamma\tau}{2\gamma\tau} > 1$, so $\delta \alpha$ can never be large enough to ensure that $Q_1^* > \overline{Q}_1$.

Using Lemma 5 that shows that $\frac{\partial (q_1^* + q_2^*)}{\partial Q_1} < 0$ if $Q_1 < \overline{Q}_1$ and $\frac{\partial (q_1^* + q_2^*)}{\partial Q_1} = 1$ if $Q_1 \ge \overline{Q}_1$, we have the following result.

Proposition 1: (The effect of a retrospective benchmark on output) Using a retrospective benchmark for excessive pricing raises Q_1 above the monopoly level Q^M , but lowers the period 2 aggregate output below the Cournot level, $q_1^C + q_2^C$. When $Q_1^* < \overline{Q}_1$ (p_1 is excessive), the expansion of output in period 1 exceeds the contraction of aggregate output in period 2. When $Q_1^* > \overline{Q}_1$ (p_1 is not excessive), the expansion of output in period 1 is equal to the contraction of aggregate output in period 2.

Proposition 1 shows that from the perspective of consumers, using a retrospective benchmark to assess whether the pre-entry price of the incumbent involves a trade-off between restraining the monopoly power of firm 1 in period 1, and softening competition in period 2 after entry takes place. The expansion of output in period 1 exceeds the reduction of output in period 2 when p_1 is excessive, but the two are equal when p_1 is not excessive. Now recall that by Assumption A1, demand is either concave or not too convex. If demand is concave or linear, the result that the expansion of output in period 1 is larger or equal to the contraction of output in period 2 implies that p_1 decreases more than p_2 increases. By continuity, p_1 also decreases more than p_2 increases, so long as demand is not too convex.

Proposition 2: (Comparative statics of Q_1^*) Q_1^* increases with the discounted probability of entry in period 2, $\delta \alpha$, but is independent of $\gamma \tau$ when $Q_1^* > \overline{Q}_1$ (p_1 is not excessive).

Proof: See the Appendix.

Intuitively, when $Q_1^* < \overline{Q}_1$ (p_1 is excessive), an increase in $\delta \alpha$ implies that entry is more likely, in which case firm 1 may have to pay a fine. Hence firm 1 has a stronger incentive to expand Q_1 and thereby relax the constraint on its period 2 output. When $Q_1^* > \overline{Q}_1$, p_1 is no longer excessive because firm 1 keeps its period 2 output below its Cournot best-response function to ensure that $q_1^* + q_2^* = Q_1$. Nonetheless, an increase in $\delta \alpha$, which makes it more likely that q_1^* will be constrained in period 2, induces firm 1 to expand Q_1 because an increase in Q_1 relaxes this constraint on q_1^* and allows firm 1 to move closer to its Cournot best-response function.

The fact that firm 1 expands Q_1 as $\delta \alpha$ increases means that consumers benefit from the prohibition of excessive pricing before entry takes place, especially when the probability of entry is high. This result is interesting because, as mentioned in the Introduction, it is often argued that when the probability of entry is high, there is no reason to intervene in excessive pricing cases, since "the market will correct itself." This argument, however, ignores the harm to consumers before entry occurs and simply says that this harm is not going to last for a long time. While this is true, our analysis shows that nonetheless, the retrospective benchmark that we consider restrains the dominant firm's pre-entry behavior and is therefore pro-competitive, particularly when the probability of entry is high.

Proposition 2 also shows that, as might be expected, the expected fine, $\gamma\tau$, has no effect on Q_1^* when p_1 is not excessive. When p_1 is excessive, i.e., $Q_1^* < \overline{Q}_1$, the effect of $\gamma\tau$ on Q_1^* is less clear because an increase in $\gamma\tau$ affects Q_1^* both directly through the expected fine that firm 1 may have to pay if p_1 is excessive, as well as through its effect on the equilibrium in period 2. In the next subsection, we show that when demand is linear an increase in $\gamma\tau$ induces firm 1 to expand Q_1^* when p_1 is excessive.

2.3 The linear demand case

In this section we derive additional results by assuming that the demand function is linear and given by p = a - Q. In particular, this assumption allows us to obtain closed-form solutions, which facilitate the analysis, and make it possible to evaluate the overall effect of the prohibition of excessive pricing on consumers.

Absent entry in period 2, firm 1 produces the monopoly output, $Q^M = \frac{A}{2}$, where $A \equiv a - c$, and earns the monopoly profit, $\pi^M = \left(\frac{A}{2}\right)^2$. If entry takes place, p_1 can be deemed excessive if it exceeds p_2 , i.e., $a - (q_1 + q_2) < a - Q_1$, or $q_1 + q_2 > Q_1$. Hence, the period 2 profits of the two firms are,

$$\pi_1(q_1, q_2) = \begin{cases} (A - q_1 - q_2)q_1, & q_1 + q_2 \le Q_1, \\ (A - q_1 - q_2)q_1 - \gamma\tau \left[(a - Q_1) - (a - q_1 - q_2) \right]Q_1, & q_1 + q_2 > Q_1, \end{cases}$$

and

$$\pi_2(q_1, q_2) = (A - q_1 - q_2)q_2.$$

The next result characterizes the resulting equilibrium in period 2.

Lemma 8: (The post-entry equilibrium in the linear demand case) The equilibrium in period 2 when firm 2 enters is $\left(\frac{A-2\gamma\tau Q_1}{3}, \frac{A+\gamma\tau Q_1}{3}\right)$ if $Q_1 < \frac{2A}{3+\gamma\tau} \equiv \overline{Q}_1$ and $(2Q_1 - A, A - Q_1)$ if $\frac{2A}{3+\gamma\tau} \leq Q_1 < \frac{2A}{3}$. Firm 1 never sets $Q_1 > \frac{2A}{3}$ because $Q_1 > \frac{2A}{3}$ is not excessive, so lowering it towards $Q^M = \frac{A}{2}$ increases Firm 1's profit.

Proof: See the Appendix.

Lemma 8 implies that the period 1 price, p_1 , is excessive when $Q_1 \leq \frac{2A}{3+\gamma\tau} \equiv \overline{Q}_1$, because

then $q_1^* + q_2^* = \frac{2A - \gamma \tau Q_1}{3} > Q_1$. When $\frac{2A}{3 + \gamma \tau} \le Q_1 < \frac{2A}{3}$, firm 1 sets q_1^* such that $p_2 = p_1$, to ensure that p_1 will not be excessive. It is easy to verify that the critical value of Q_1 below which p_1 is excessive, $\overline{Q}_1 \equiv \frac{2A}{3 + \gamma \tau}$, satisfies equation (3) when p = a - Q.

Given the equilibrium in period 2, the expected discounted profit of firm 1 in period 1 is

$$\Pi_{1}(Q_{1}) = \begin{cases} (A - Q_{1})Q_{1} + \delta(1 - \alpha)\left(\frac{A}{2}\right)^{2} + \delta\alpha\left[\left(\frac{A}{3}\right)^{2} - \frac{\gamma\tau Q_{1}(7A - (9 + \gamma\tau)Q_{1})}{9}\right], & Q_{1} < \frac{2A}{3 + \gamma\tau}, \\ (A - Q_{1})Q_{1} + \delta(1 - \alpha)\left(\frac{A}{2}\right)^{2} + \delta\alpha(A - Q_{1})(2Q_{1} - A), & \frac{2A}{3 + \gamma\tau} \leq Q_{1} \leq \frac{2A}{3}. \end{cases}$$

$$(5)$$

Firm 1 sets Q_1 to maximize this expression. In the next proposition we characterize the choice of Q_1 and the resulting equilibrium in period 2.

Proposition 3: (The equilibrium in the linear demand case) Suppose that p = a - Q and assume that $\delta \alpha \leq 0.9$ (this assumption ensures that $\Pi_1(Q_1)$ is piecewise concave). Then,

$$Q_{1}^{*} = \begin{cases} \frac{A}{2} \begin{bmatrix} \frac{9-7\delta\alpha\gamma\tau}{9-\delta\alpha\gamma\tau(9+\gamma\tau)} \end{bmatrix}, & \delta\alpha < Z(\gamma\tau), \\ \frac{A}{2} \begin{bmatrix} \frac{1+3\delta\alpha}{1+2\delta\alpha} \end{bmatrix}, & \delta\alpha \ge Z(\gamma\tau), \end{cases}$$
(6)

where

$$Z\left(\gamma\tau\right) \equiv \frac{1 + 7\gamma\tau\left(2 - \gamma\tau\right) - \left(1 + \gamma\tau\right)\sqrt{1 + 5\gamma\tau\left(2 + \gamma\tau\right)}}{2\gamma\tau\left(1 + 11\gamma\tau\right)}.$$

 p_1 is excessive if $\delta \alpha < Z(\gamma \tau)$, but not otherwise. Note that so long as $0 < \delta \alpha < 1$, $\frac{A}{2} < Q_1^* < \frac{2A}{3}$, implying that Q_1^* is above the monopoly level, but below the aggregate Cournot level. The resulting equilibrium quantities in period 2 are given by

$$q_{1}^{*} = \begin{cases} \frac{A(3(1-\gamma\tau)-\delta\alpha\gamma\tau(3-\gamma\tau))}{9-\delta\alpha\gamma\tau(9+\gamma\tau)}, & \delta\alpha < Z(\gamma\tau), \\ \frac{\delta\alpha A}{1+2\delta\alpha}, & \delta\alpha \ge Z(\gamma\tau), \end{cases}$$
(7)

and

$$q_2^* = \begin{cases} \frac{3A(2+\gamma\tau)(1-\delta\alpha\gamma\tau)}{2(9-\delta\alpha\gamma\tau(9+\gamma\tau))}, & \delta\alpha < Z(\gamma\tau), \\ \frac{A(1+\delta\alpha)}{2(1+2\delta\alpha)}, & \delta\alpha \ge Z(\gamma\tau). \end{cases}$$
(8)

Proof: See the Appendix.

Proposition 3 fully characterizes the equilibrium and allows us to establish the precise conditions under which p_1 is excessive and examine how the equilibrium responds to changes in the discounted probability of entry, $\delta \alpha$, and the expected fine, $\gamma \tau$. When $\delta \alpha < Z(\gamma \tau)$ ($\delta \alpha$ is small) firm 1 sets Q_1 such that p_1 ends up being excessive. But when $\delta \alpha \geq Z(\gamma \tau)$ ($\delta \alpha$ is large), firm 1 sets Q_1 such that p_1 is not excessive. Plotting $Z(\gamma \tau)$ with Mathematica reveals that $Z'(\gamma \tau) < 0$, with Z(1) = 0. Hence, the latter case, where p_1 is not excessive, becomes more likely as $\gamma \tau$ increases. The implication is that either an increase in the discounted probability of entry, $\delta \alpha$, or an increase in the expected fines, $\gamma \tau$, that firm 1 pays when p_1 is excessive, induce firm 1 to expand Q_1 to ensure that p_1 is not excessive.

Moreover, (6) implies that $\frac{\partial Q_1^*}{\partial (\delta \alpha)} > 0$ as we already proved in Proposition 2. In addition, (6) implies that $\frac{\partial Q_1^*}{\partial (\gamma \tau)} = \frac{A(18\delta \alpha (1+\gamma \tau)-7(\delta \alpha \gamma \tau)^2)}{2(9-\delta \alpha \gamma \tau (9+\gamma \tau))^2} > 0$ when $\delta \alpha < Z(\gamma \tau)$ (p_1 is excessive) and $\frac{\partial Q_1^*}{\partial (\gamma \tau)} = 0$, when $\delta \alpha > Z(\gamma \tau)$ (p_1 is not excessive). Roughly speaking, an increase in $\gamma \tau$ means that firm 1 would have to pay a higher expected per-unit fine when entry occurs, so it has a stronger incentive to expand Q_1 in order to lower the total expected fine it pays.

2.4 Welfare in the linear demand case

We now turn to the welfare implications of using the post-entry price as a benchmark to assess whether the dominant firm's pre-entry price was excessive. When demand is linear, consumers' surplus, given an aggregate output Q, is

$$CS(Q) = \int_0^Q (a-x) \, dx - (a-Q) \, Q = \frac{Q^2}{2}.$$

Absent entry, firm 1 is a monopoly in period 2 and produces the monopoly output $\frac{A}{2}$. With entry, the equilibrium in period 2 is characterized in Lemma 8. The aggregate output is $\frac{2A-\gamma\tau Q_1^*}{3}$ if $\delta \alpha < Z(\gamma \tau)$ (p_1 is excessive), and Q_1^* if $\delta \alpha \geq Z(\gamma \tau)$ (p_1 is not excessive), where Q_1^* is given by (6). (In the latter case, p_1 is not excessive precisely because firm 1 sets q_1 such that $q_1^* + q_2^* = Q_1$). Since the probability of entry is α , the overall expected discounted consumers' surplus over the two periods is given by

$$CS\left(Q_{1}^{*}\right) = \begin{cases} \frac{\left(Q_{1}^{*}\right)^{2}}{2} + \frac{\delta\left(1-\alpha\right)}{2}\left(\frac{A}{2}\right)^{2} + \frac{\delta\alpha}{2}\left(\frac{2A-\gamma\tau Q_{1}^{*}}{3}\right)^{2}, & \delta\alpha < Z\left(\gamma\tau\right), \\ \frac{\left(Q_{1}^{*}\right)^{2}}{2} + \frac{\delta\left(1-\alpha\right)}{2}\left(\frac{A}{2}\right)^{2} + \frac{\delta\alpha}{2}\left(Q_{1}^{*}\right)^{2}, & \delta\alpha \ge Z\left(\gamma\tau\right), \end{cases}$$
(9)

It is obvious that $CS(Q_1^*)$ increases with $\delta \alpha$ because total output in period 2 when entry occurs exceeds total output absent entry. In the next proposition we examine how $CS(Q_1^*)$ is affected by $\gamma \tau$. **Proposition 4:** (The comparative statics of consumers' surplus with respect to $\gamma \tau$ in the linear demand case) Suppose that p = a - Q. Then, an increase in the expected per-unit fine, $\gamma \tau$, raises consumers' surplus when $\delta \alpha < Z(\gamma \tau)$ (p_1 is excessive) and has no effect when $\delta \alpha \geq Z(\gamma \tau)$ (p_1 is not excessive).

Proof: See the Appendix.

We have already shown that the prohibition of excessive pricing involves a trade-off between a higher pre-entry output and a lower post-entry output. Proposition 4 allows us to examine the overall effect on consumers' surplus. To understand the proposition, note that $\gamma \tau = 0$ is equivalent to having no prohibition of excessive pricing. Since the proposition shows that consumers' surplus increases with $\gamma \tau$ when p_1 is excessive and is not affected by $\gamma \tau$ when p_1 is not excessive, it follows that the prohibition of excessive pricing benefits consumers, and more so as $\gamma \tau$ increases.

It is important to stress that Proposition 4 should be interpreted cautiously, because our model abstracts from a number of factors, that are likely to be relevant in reality, like the cost of detecting excessive prices, the legal costs involved with court cases, and the potential effect of the prohibition of excessive prices on the firm's incentive to invest. Still, Proposition 4 shows that, at least in the context of quantity competition and linear demand, the effects that we identify - a decrease in p_1 and an increase in p_2 - benefit consumers on balance.

3 A retrospective benchmark under price competition

In this section we consider the same model as in Section 2, except that now we assume that firms set prices rather than quantities. In the absence of a prohibition of excessive pricing, firm 1 sets the monopoly price in period 1 and also in period 2 if there is no entry, but if entry occurs, both firms charge a price equal to marginal cost c.

When excessive pricing is prohibited, the above strategies are no longer an equilibrium because following entry, the equilibrium price drops, so firm 1's price in period 1 may be deemed excessive. This possibility affects firm 1's behavior. To characterize the resulting equilibrium, it is important to note that unlike quantity competition, which features a single market clearing price, now the two firms may charge different prices. We will assume in what follows that only firm 1's price serves as a benchmark to evaluate whether firm 1's price in period 1 was or was not excessive, but only if firm 1 actually makes sales in period 2 (otherwise firm 1's price is merely theoretic). Let Q(p) denote the demand function (previously we worked with the inverse demand function, p(Q)), and let p_1 and p_{12} denote the prices that firm 1 sets in periods 1 and 2, and p_{22} the price that firm 2 sets in period 2 if it enters the market. Absent entry, firm 1 simply sets in period 2 the monopoly price $p^M \equiv \arg \max Q(p_{12})(p_{12} - c)$ and earns the monopoly profit, $\pi^M \equiv Q(p^M)(p^M - c)$. If entry occurs, firms 1 and 2 set prices p_{12} and p_{22} and consumers buy from the lowest price firm. If $p_{12} = p_{22}$, consumers buy from the more efficient firm.²² In our case, the more efficient firm in period 2 is firm 2, since firm 1 may have to pay a fine on its period 1 price. The profit functions in period 2 following entry are given by

$$\pi_1(p_{12}, p_{22}) = \begin{cases} 0, & p_{12} \ge p_{22}, \\ Q(p_{12})(p_{12} - c) - \gamma \tau [p_1 - p_{12}]^+ Q(p_1), & p_{12} < p_{22}, \end{cases}$$
(10)

and

$$\pi_2(p_{12}, p_{22}) = \begin{cases} Q(p_{22})(p_{22} - c), & p_{12} \ge p_{22}, \\ 0, & p_{12} < p_{22}, \end{cases}$$
(11)

where $[p_1 - p_{12}]^+ \equiv \max \{p_1 - p_{12}, 0\}$ because firm 1 pays a fine in period 2 only if it makes sales and only if its price in period 1 exceeds its price in period 2: $p_1 > p_{12}$. We shall assume that the bottom line in (10) is quasi-concave in p_{12} and the top line in (11) is quasi-concave in p_{22} . Let $\underline{p}(p_1)$ be the value of p_{12} at which the bottom line in (10) vanishes when $p_1 > p_{12}$. That is, $\underline{p}(p_1)$ is the value of p_{12} at which $Q(p_{12})(p_{12} - c) = \gamma \tau (p_1 - p_{12}) Q(p_1)$.²³ Note that $\underline{p}(p_1)$ is increasing with $\gamma \tau$ and equal to c when $\gamma \tau = 0$. The intuition for this is that an increase in $\gamma \tau$ raises the expected fine that firm 1 has to pay, and hence, raises the price that firm 1 must charge in period 2 in order to break even.

Since firm 1 can guarantee itself a profit of 0 in period 2 by setting a price above p^{M} (setting a price above p^{M} is a dominated strategy for firm 2, so any price above p^{M} ensures firm 1 a profit of 0), firm 1 will never set a price below $\underline{p}(p_{1})$. Moreover, $\underline{p}(p_{1}) > c$, since at $p_{12} = c$, the bottom line of (10) is equal to $-\gamma \tau Q(c)(p_{1} - p_{12})Q(p_{1}) < 0$. Hence, firm 2 is indeed more efficient than firm 1 since it can make a profit at prices between $p(p_{1})$ and c, while firm 1 cannot.

In the next proposition we report the resulting equilibrium:

²²This tie-breaking rule is standard (see e.g., Deneckere and Kovenock, 1996).

²³The bottom line of (10) has two roots since $Q(p_{12})(p_{12}-c)$ is an inverse U-shape function of p_{12} , while $\gamma \tau (p_1 - p_{12}) Q(p_1)$ is a decreasing line. The relevat root is the smaller between the two since firm 1 does not charge a price above the monopoly price, p^M , which maximizes $Q(p_{12})(p_{12}-c)$.

Proposition 5: (The equilibrium under price competition) Suppose that firms 1 and 2 have the same marginal cost c and compete by setting prices. Moreover, assume that firm 1's price in period 1 is deemed excessive if firm 1 makes sales in period 2 at a price below its period 1 price. Then, when entry occurs, both firms charge $\underline{p}(p_1)$ and all consumers buy from firm 2. Since firm 1 makes no sales in period 2, its period 1 price cannot be deemed excessive, and hence it sets the monopoly price, p^M , in period 1.

Proposition 5 implies that the prohibition of excessive pricing harms consumers in period 2 by raising the equilibrium price, without lowering the price they pay in period 1. The reason for this is that due to the fine it may have to pay, the lowest price that firm 1 is willing to set in period 2 is $\underline{p}(p_1)$. This allows firm 2 to monopolize the market in period 2 by charging $\underline{p}(p_1)$. Since $\underline{p}(p_1) > c$, consumers pay a higher price than they would have paid absent a prohibition of excessive pricing. While the prohibition of excessive pricing also raises the equilibrium price in period 2 under quantity competition, here it does not help consumers in period 1 because firm 1 makes no sales in period 2 when firm 2 enters, and hence it can safely set the monopoly price, p^M , in period 1. Under quantity competition, firm 1 does make sales in period 2 even when firm 2 enters, and therefore has an incentive to expand output in period 1 in order to lower its period 1 price and hence relax the constraint on its behavior in period 2.

Proposition 5 depends on our assumption that firm 2's cost is equal to firm 1's cost. Next, we relax this assumption and allow firm 2's cost, c_2 , to be randomly drawn from the interval $[0, p^M]$, according to a distribution function $f(c_2)$ with a cumulative distribution $F(c_2)$. Now, firm 2 may not enter the market when c_2 is large; hence we will now interpret α as the probability that firm 2 is born.

With probability $1 - \alpha$, firm 2 is not born and firm 1 is a monopoly in period 2 and charges the monopoly price, p^M . With probability α , firm 2 is born and needs to decide whether to enter the market. When $c_2 < c$, firm 2 enters the market and monopolizes it even without a prohibition of excessive pricing. The prohibition though allows firm 2 to raise its price from c to $\underline{p}(p_1)$. When $c_2 \in [c, \underline{p}(p_1)]$, firm 2 enters the market and monopolize it by charging $\underline{p}(p_1)$. Entry though is inefficient and is feasible only because it is unprofitable for firm 1 which is more efficient to price below $\underline{p}(p_1)$ due to the prohibition of excessive pricing. When $c_2 \in (\underline{p}(p_1), p^M]$, firm 1 maintains its monopoly position in period 2 and charges c_2 , exactly as it does in the absence of an antitrust prohibition of excessive pricing. Production is now efficient since the market is served by the more efficient firm 1.

In sum, when firm 2 is born, it monopolizes the market when $c_2 \leq \underline{p}(p_1)$, in which case the prohibition of excessive pricing harms consumers in period 2 because it raises the price from max $\{c, c_2\}$ to $\underline{p}(p_1)$. When $c_2 > \underline{p}(p_1)$, firm 1 remains a monopoly and the prohibition of excessive pricing has no effect on consumers. Interestingly, the prohibition of excessive pricing harms consumers precisely when entry takes place. The reason is that absent a prohibition of excessive pricing, potential entry would have led to an even lower price.

We now turn to p_1 , which is the price that firm 1 sets in period 1. This price is chosen to maximize firm 1's expected discounted profit, given by

$$\Pi(p_{1}) = Q(p_{1})(p_{1}-c) + \delta(1-\alpha)\pi^{M} + \delta\alpha \int_{\underline{p}(p_{1})}^{p^{M}} \left[Q(c_{2})(c_{2}-c) - \gamma\tau [p_{1}-c_{2}]^{+}Q(p_{1})\right] dF(c_{2})$$

$$= Q(p_{1})(p_{1}-c) + \delta(1-\alpha)\pi^{M} + \delta\alpha \int_{\underline{p}(p_{1})}^{p^{M}} Q(c_{2})(c_{2}-c) dF(c_{2})$$

$$-\delta\alpha\gamma\tau \int_{\underline{p}(p_{1})}^{p_{1}} (p_{1}-c_{2})Q(p_{1}) dF(c_{2}).$$

In the next proposition, we characterize the equilibrium value of p_1 and examine how the retrospective benchmark affects consumers.

Proposition 6: (The effect of a retrospective benchmark under price competition when firms have asymmetric costs) Suppose that firms 2's cost is randomly drawn from the interval $[0, p^M]$, and that firm 1's price in period 1, p_1 , is deemed excessive if firm 1 makes sales in period 2 at a price below p_1 . Then, the prohibition of excessive pricing raises prices in period 2 when firm 2 enters the market and has no effect on prices when firm 1 remains a monopoly. In period 1 the prohibition of excessive pricing lowers p_1 . Moreover, p_1 is decreasing with $\delta \alpha$, which is the discounted probability that firm 2 is born.

Proof: See the Appendix.

Proposition 6 shows that, as in the case of quantity competition, using a retrospective benchmark to enforce the prohibition of excessive pricing involves tradeoff between lower prices in period 1 and potentially higher prices post entry. Firm 1 lowers its pre-entry price in order to lower its excess revenue in period 1 on which it may pay a fine in period 2. This relaxes the constraint on firm 1's price in period 2. But then, the fine that firm 1 may have to pay increases its cost in period 2 and hence allows firm 2 to set a higher price when it monopolizes the market in period 2.

4 A contemporaneous benchmark

Another price benchmark which is often used in practice to assess whether the price of a dominant firm is excessive is the price that the same firm is contemporaneously charging in other markets. This benchmark was used for example in the British Leyland and the Napp cases that were mentioned in the Introduction.²⁴

We will now study the competitive effects of a contemporaneous benchmark for excessive pricing under both quantity and price competition. To this end, we will assume that firm 1 is a monopoly in market 1, but faces competition from firm 2 in market 2. Both firms have a common marginal cost $c.^{25}$ In both markets, the demand system is derived from the preferences of a representative agent whose utility function is given by

$$U(q_1, q_1, m) = a(q_1 + q_2) - \frac{q_1^2 + q_2^2 + 2bq_1q_2}{2} + m,$$
(12)

where $b \in [0, 1]$ is a measure of product differentiation and m is the monetary expenditure on all other goods. The demand system in market 2 is derived by maximizing the representative agent's utility subject to his budget constraint given by $p_1q_1 + p_2q_2 + m = I$, where I is the agent's income. The demand in market 1, where firm 1 is a monopoly, is derived similarly but subject to the constraint that $q_2 = 0$.

4.1 Quantity competition

Let Q_1 and p_1 be the output and price of firm 1 in market 1, and let q_1 and q_2 be the outputs of firms 1 and 2 in market 2, and p_{12} and p_{22} be their corresponding prices. The inverse demand functions are then given by:

$$p_1 = a - Q_1, \qquad p_{12} = a - q_1 - bq_2, \qquad p_{22} = a - q_2 - bq_1.$$
 (13)

²⁴ Another example is the Israeli potash case mentioned in the Introduction. The Central District Court held that Dead Sea Works not only raised its price substantially in 2008-9 relative to 2007, but also charged a much higher price in Israel than overseas. See Class Action (Central District Court) 41838-09-14 Weinstein v. Dead Sea Works, Inc. (Nevo, 29.1.2017).

²⁵ If firm 1 has a different cost in markets 1 and 2, one would have to compare it price-cost margins across the two markets instead of simply comparing its prices. It should be noted that in real-life cases, establishing the relevant cost in each market is typically complicated and often contentious.

Notice that when b = 1, the model is identical to the model in Section 2, except that instead of having two time periods, we now have two separate markets. The main implications in terms of the analysis is that now, Q_1 , q_1 , and q_2 , are set simultaneously, instead of Q_1 being set before q_1 and q_2 . Recalling that $A \equiv a - c$, the profit functions of firms 1 and 2 are given by

$$\Pi_{1}(Q_{1},q_{1},q_{2}) = \begin{cases} (A-Q_{1})Q_{1} + (A-q_{1}-bq_{2})q_{1}, & q_{1}+bq_{2} \leq Q_{1} \\ (A-Q_{1})Q_{1} + (A-q_{1}-bq_{2})q_{1} - \gamma\tau \left[(a-Q_{1}) - (a-q_{1}-bq_{2})\right]Q_{1}, & q_{1}+bq_{2} > Q_{1} \end{cases}$$

and

$$\Pi_2(q_1, q_2) = (A - q_2 - bq_1)q_2.$$

To ensure that $\Pi_1(Q_1, q_1, q_2)$ is concave we will assume that $\gamma \tau \leq 0.8$. We now characterize the Nash equilibrium.

Proposition 7: (The equilibrium in the contemporaneous benchmark case) Suppose that firm 1 is a monopoly in market 1, but competes with firm 2 in market 2 and assume that the inverse demand functions are given by (13). Then, the equilibrium is given by

$$Q_1^* = \frac{A\left(2-b\right)\left(2-\gamma\tau+b\left(1-\gamma\tau\right)\right)}{\left(2-b^2\right)H+4\left(1-\gamma\tau\right)},\tag{14}$$

$$q_1^* = \frac{A\left(4 - 6\gamma\tau - H\right)}{\left(2 - b^2\right)H + 4\left(1 - \gamma\tau\right)}, \qquad q_2^* = \frac{A\left(H + 2\left(1 - \gamma\tau\right) - b\left(2 - 3\gamma\tau\right)\right)}{\left(2 - b^2\right)H + 4\left(1 - \gamma\tau\right)},\tag{15}$$

where $H \equiv 2 - 2\gamma\tau - (\gamma\tau)^2$, if $\gamma\tau < \frac{b(2-b)}{4+b-2b^2}$ and by

$$Q_1^* = \frac{A\left(4+b-2b^2\right)}{8-3b^2}, \qquad q_1^* = \frac{A\left(4-3b\right)}{8-3b^2}, \qquad q_2^* = \frac{2A\left(2-b\right)}{8-3b^2}.$$
(16)

if $\gamma \tau \geq \frac{b(2-b)}{4+b-2b^2}$. When $\gamma \tau < \frac{b(2-b)}{4+b-2b^2}$, p_1 exceeds p_{12} , in which case p_1 is excessive. Then, p_1 decrease with $\gamma \tau$ while p_{12} and p_{22} increase with $\gamma \tau$.

Proof: See the Appendix.

Proposition 7 shows that p_1 is excessive only when $\gamma \tau < \frac{b(2-b)}{4+b-2b^2}$. When $\gamma \tau \ge \frac{b(2-b)}{4+b-2b^2}$, the prohibition of excessive pricing completely deters firm 1 from setting an excessive p_1 . The critical value $\frac{b(2-b)}{4+b-2b^2}$ is increasing with b and equal to 0 when b = 0. In the latter case, firm 1 does not compete with firm 2 in market 2 and hence it sets the monopoly price in both markets 1 and 2, so p_1 is not excessive. As b increases, competition between firms 1 and 2 intensifies, so firm 1 has an

incentive to expand its output in market 2. Consequently, p_{12} drops below p_1 and hence p_1 may be deemed excessive. Firm 1 responds by expanding Q_1 to lower p_1 and limit the gap between p_1 and p_{12} , but by doing so, it sacrifices some of its profit in market 1. The willingness of firm 1 to expand Q_1 increases when $\gamma \tau$ increases. When $\gamma \tau = \frac{b(2-b)}{4+b-2b^2}$, firm 1 expands Q_1 to the point where p_1 is no longer excessive.

Proposition 7 also shows that an increase in $\gamma \tau$ induces firm 1 to further expand Q_1 and contract q_1 in order to lower the gap between p_1 and p_{12} and thereby lower its excessive revenue in market 1 on which it may pay a fine. This benefits consumers in market 1 but harms firm 1's consumers in market 2. Under quantity competition, the strategies of firms 1 and 2 in market 2 are strategic substitutes, so firm 2 expands its own output. The contraction of firm 1's output has a bigger effect on p_{22} than the expansion of firm 2's output, so overall firm 2's price increases making firm 2's consumers worse off.

Noting that when excessive pricing is not prohibited $\gamma \tau = 0$, it follows that a contemporaneous benchmark involves a tradeoff between the welfare of consumers in markets 1 and 2. To examine the overall effect on consumers, note that if we substitute for m from the budget constraint $p_1q_1 + p_2q_2 + m = I$ into (12) and use the inverse demand functions (13), overall consumers' surplus is given by

$$CS(Q_1, q_1, q_2) = \frac{Q_1^2}{2} + \frac{q_1^2 + q_2^2 + 2bq_1q_2}{2}$$

Substituting for the equilibrium quantitates from Proposition 7 into $CS(Q_1, q_1, q_2)$, yields the overall consumers' surplus in equilibrium, $CS^* \equiv CS(Q_1^*, q_1^*, q_2^*)$, where CS^* is a ratio of two 4th degree polynomials in $\gamma\tau$ and b. Absent a prohibition of excessive pricing, consumers' surplus is given by $CS_0^* \equiv CS^*|_{\gamma\tau=0}$. Hence, we can study the effect of a contemporaneous benchmark on consumers by looking at $CS^* - CS_0^*$. The next figure shows $CS^* - CS_0^*$ as a function of $\gamma\tau$ and b.



Figure 3: The effect of a contemporeneous bechmark for excessive pricing on consumers under quantity competition

As Figure 3 shows, p_1 is excessive only when $\gamma \tau < \frac{b(2-b)}{4+b-2b^2}$. Then, using a contemporaneous benchmark to determine whether p_1 is excessive enhances consumers' surplus when $\gamma \tau$ is relatively high, but lowers consumers' surplus when $\gamma \tau$ is relatively small. The boundary between the regions increases with b. To see the intuition, suppose that $b = \gamma \tau = 0$, and consider an increase in b. Then competition intensifies in market 2, which benefits consumers in market 2. But then p_{12} is lower than p_1 , so p_1 is excessive and firm 1 may pay a fine. If $\gamma \tau$ increases from 0, firm 1 has an incentive to lower the gap between p_1 and p_{12} and hence it expands output in market 1 and contract output in market 2. As Proposition 7 shows, consumers in market 1 become better off while consumers in market become worse off. When $\gamma \tau$ is low, the former effect outweighs the latter, so overall, consumers become better off. When $\gamma \tau$ increases towards $\frac{b(2-b)}{4+b-2b^2}$, the gap between firm 1's prices in markets 1 and 2 shrinks to 0 and hence the effect on their surplus cancel each other out. But since firm 2's consumers are worse off overall consumers' surplus drops.

A contemporaneous benchmark for excessive pricing is reminiscent of contemporaneous MFN's, which prevent firms from offering selective discounts to some consumers. Besanko and Lyon (1992) show that contemporaneous MFN's relax price competition, though in equilibrium firms may not wish to adopt them unilaterally. Their model differs from ours in that they assume that firms compete in both markets (the market for shoppers and the market for non-shoppers in their model), while in our model, firm 1 is a monopoly in market 1. Moreover, they assume that

an MFN renders price discriminate impossible, while in our model, firm 1 can still charge different prices in the two markets, but then may have to pay a fine with probability γ . In terms of results, Besanko and Lyon (1992) show that MFN's harm consumers because they raise the average price across the two markets, while in our framework a prohibition of excessive pricing benefits consumers in the monopoly market and harms consumers in the benchmark market.

4.2 Price competition

To study the case where firms 1 and 2 compete in market 2 by setting prices, we first invert the inverse demand system (13) to obtain the following demand system:

$$Q_1 = a - p_1,$$
 $q_1 = a(1+b) - \frac{p_1 - bp_2}{1 - b^2},$ $q_2 = a(1+b) - \frac{p_2 - bp_1}{1 - b^2}$

Using this demand system, we repeat the same steps as in the case of quantity competition. The results are qualitatively similar and are reported in the Appendix. The next figure shows $CS^* - CS_0^*$ as a function of $\gamma\tau$ and b. Now, p_1 is excessive when $\gamma\tau < \frac{b(2+b)}{4+b-2b^2}$ and as in the case of quantity competition, using a contemporaneous benchmark to determine whether p_1 is excessive enhances consumers' surplus when $\gamma\tau$ is relatively high, but lowers consumers' surplus when $\gamma\tau$ is relatively small.



Figure 4: The effect of a contemporeneous bechmark for excessive pricing on consumers under price competition

5 Conclusion

We have examined the competitive effects of the prohibition of excessive pricing by a dominant firm. A main problem when implementing this prohibition is to establish an appropriate competitive benchmark to assess whether the dominant firm's price is indeed excessive. In this paper we have studied two such benchmarks which are used in practice: a retrospective benchmark, where the price that the dominant firm charges following entry into the market is used to determine whether its pre-entry price was excessive, and a contemporaneous benchmark, where the price that the dominant firm is charging in a more competitive market is used to determine whether its price in a market where it is dominant is excessive. If the dominant firm's price is deemed excessive, the firm pays a fine proportional to its excess revenue, which is equal to the difference between the actual price and the benchmark price, times the firm's output given the excessive price.

We find that the two benchmarks lead to a tradeoff: they restrain the dominant firm's behavior when its acts as a monopoly, but soften the firm's behavior in the benchmark market (the post-entry market in the retrospective benchmark case and the more competitive market in the contemporaneous benchmark case). We show that when the dominant firm and the rival compete in the benchmark market by setting quantities and products are homogenous, the pro-competitive effect of a retrospective benchmark in the monopoly market outweight the corresponding anticompetitive effect in the benchmark market. Hence, a retrospective benchmark for excessive pricing benefits consumers overall. By contrast, under price competition with homogenous products and symmetric costs, a retrospective benchmark softens competition post-entry without lowering the pre-entry price, implying that consumers are overall worse off. We also show that when a contemporaneous benchmark, benefits consumers when the expected fine that the firm pays when its price in the monopoly market is deemed excessive is relatively low, but harms consumers when the expected fine is relatively high. These results hold under both quantity and price competition. These results indicate that the overall competitive effect of the prohibition of excessive pricing depends on the precise nature of competition as well as on the expected fines that are imposed when the firm's price is deemed excessive.

In addition, we also show that using a retrospective benchmark to enforce the prohibition of excessive pricing may actually promote entry into the market as it induces the incumbent firm to behave more softly once entry takes place. This soft behavior may actually enable an inefficient entrant to successfully enter the market. While our analysis highlights two new effects that were not discussed earlier, we abstract from many considerations which are likely to be important in real-life cases. For example, our model does not take into account the incentive of firms to invest in R&D, advertising, or product quality, hold inventories, offer a variety of products, choose locations and other non-price decisions that affect competition and consumer welfare. Our model also abstracts from the cost of litigation and other legal costs, as well as from demand and cost fluctuations which make it harder to compare prices across different time periods. Hence, more research is needed before we fully understand the competitive implications of the prohibition of excessive pricing. Our results show, however, highlights the competitive effect of the prohibition of excessive pricing on the price in the monopoly market and on the benchmark price. These effects were not considered earlier in the discussion about the excessive pricing.

Our analysis can be extended in a number of ways. We mention here a few. First, it is possible to endogenize the probability of entry, α , by assuming that the entrant has to bear an entry cost, drawn from some known interval; entry then occurs only if the entrant's profit exceeds its entry cost. In such a setting, the dominant firm will have to take into account the effects of its pre-entry output on the post-entry equilibrium and hence on the probability of entry. Second, it is possible to assume that the probability that the dominant firm is convicted, γ , increases with the gap between the pre- and post-entry prices. For instance, $\gamma = 0$ if the gap is below Δ , but $\gamma > 0$ if the gap exceeds Δ . It should be interesting to examine how consumers' surplus changes with Δ . Third, one can study a model in which the marginal cost of the dominant firm is private information. In that case, its the period 1 output will be a signal for its cost, which will affect the incentive to charge an excessive price. Fourth, one can examine the competitive effects of the prohibition of excessive pricing under alternative types of competition, like price competition with product differentiation, and examine how factors like the extent of product differentiation affect matters. We leave these extensions and others for future research.

6 Appendix

Following are the proofs of Lemmas 1, 2, 4, 5, 7 and 8, and Propositions 2-4, 6 and 7 and the characterization of the equilibrium in the contemporaneous benchmark case under price competition.

Proof of Lemma 1: We begin by proving that $\pi_1(q_1, q_2)$ is concave in q_1 and $\pi_2(q_1, q_2)$ is concave in q_2 . To this end, note that differentiating the first line in $\pi_1(q_1, q_2)$ yields:

$$\frac{\partial^2 \pi_1 (q_1, q_2)}{\partial q_1^2} = 2p' (q_1 + q_2) + p'' (q_1 + q_2) q_1.$$

If $p''(\cdot) \le 0$, we are done. If $p''(q_1 + q_2) > 0$,

$$\frac{\partial^2 \pi_1 \left(q_1, q_2 \right)}{\partial q_1^2} < 2p' \left(q_1 + q_2 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + q_2 \right) < 0,$$

where the last inequality follows from Assumption A1. Hence, $\pi_1(q_1, q_2)$ is concave in q_1 when $q_1 + q_2 \leq Q_1$. The proof that $\pi_2(q_1, q_2)$ is concave in q_2 is identical.

Differentiating the second line in $\pi_1(q_1, q_2)$ yields:

$$\frac{\partial^2 \pi_1 \left(q_1, q_2 \right)}{\partial q_1^2} < 2p' \left(q_1 + q_2 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) + p'' \left(q_1 + q_2 \right) \left(q_1 + \gamma \tau Q_1 \right) + p'' \left(q_1 + q_2 \right) + p'' \left(q_$$

Again, if $p''(\cdot) \leq 0$, we are done. If $p''(q_1 + q_2) > 0$,

$$\frac{\partial^2 \pi_1 (q_1, q_2)}{\partial q_1^2} < 2p' (q_1 + q_2) + p'' (q_1 + q_2) (q_1 + \gamma \tau (q_1 + q_2)) < 2p' (q_1 + q_2) + p'' (q_1 + q_2) (1 + \gamma \tau) (q_1 + q_2) < 0,$$

where the first inequality follows because $q_1 + q_2 > Q_1$, and the last inequality follows from Assumption A1. Hence, $\pi_1(q_1, q_2)$ is also concave in q_1 when $q_1 + q_2 > Q_1$.

Since firm 2's profit is concave in q_2 , $BR_2(q_1) = r_2^C(q_1)$, where $r_2^C(q_1)$ is defined by (1). To characterize $BR_1(q_2)$, note first that $\pi_1(q_1, q_2)$ is continuous at $q_1 + q_2 = Q_1$ and is piecewise concave in q_1 (i.e., both when $q_1 + q_2 \le Q_1$, as well as when $q_1 + q_2 > Q_1$). Now,

$$\frac{\partial \pi_1 (q_1, q_2)}{\partial q_1} = \begin{cases} p(q_1 + q_2) + p'(q_1 + q_2) q_1 - c, & q_1 + q_2 \le Q_1, \\ p(q_1 + q_2) + p'(q_1 + q_2) (q_1 + \gamma \tau Q_1) - c, & q_1 + q_2 > Q_1. \end{cases}$$
(17)

Note that since $p'(q_1+q_2) < 0$, $\frac{\partial \pi_1(q_1,q_2)}{\partial q_1} < 0$ as $q_1 + q_2$ approaches Q_1 from below also implies

that $\frac{\partial \pi_1(q_1,q_2)}{\partial q_1} < 0$ as $q_1 + q_2$ approaches Q_1 from above. Together with the fact that $\pi_1(q_1,q_2)$ is continuous at $q_1 + q_2 = Q_1$ and piecewise concave, it follows that

- (i) $\pi_1(q_1, q_2)$ attains a maximum at $q_1 < Q_1 q_2$ if $\frac{\partial \pi_1(q_1, q_2)}{\partial q_1} < 0$ as $q_1 + q_2$ approaches Q_1 from below, i.e., when $p(Q_1) + p'(Q_1)(Q_1 q_2) < c$,
- (ii) $\pi_1(q_1, q_2)$ attains a maximum at $q_1 > Q_1 q_2$ if $\frac{\partial \pi_1(q_1, q_2)}{\partial q_1} > 0$ as $q_1 + q_2$ approaches Q_1 from above, i.e., when $p(Q_1) + p'(Q_1)((1 + \gamma \tau)Q_1 q_2) > c$,
- (iii) $\pi_1(q_1, q_2)$ attains a maximum at $q_1 = Q_1 q_2$ if $\frac{\partial \pi_1(q_1, q_2)}{\partial q_1} > 0$ as $q_1 + q_2$ approaches Q_1 from below, and $\frac{\partial \pi_1(q_1, q_2)}{\partial q_1} < 0$ as $q_1 + q_2$ approaches Q_1 from above, i.e., when $p(Q_1) + p'(Q_1)(Q_1 q_2) > c > p(Q_1) + p'(Q_1)((1 + \gamma \tau)Q_1 q_2).$

In case (i), p_1 is not excessive, and firm 1's best-response function is defined by $r_1^C(q_2)$. In case (ii), p_1 is excessive and firm 1's best-response function is defined by $r_1^E(q_2)$. And in case (iii), firm 1 sets q_1 to ensure that $q_1 + q_2 = Q_1$; this ensures that p_1 is not deemed excessive.

To study the slopes of the best-response functions in the (q_1, q_2) space, notice first that

$$BR'_{2}(\cdot) = -\frac{\frac{\partial \pi_{2}^{2}(q_{1}^{*}, q_{2}^{*})}{\partial q_{1} \partial q_{2}}}{\frac{\partial \pi_{2}^{2}(q_{1}^{*}, q_{2}^{*})}{\partial q_{2}^{2}}} = -\frac{p' + p'' q_{2}}{2p' + p'' q_{2}}$$

where the arguments of p' and p'' are suppressed to ease notation. Assumption A1 is sufficient to ensure that $-1 \leq BR'_2(\cdot) < 0$. The proof that $BR'_1(\cdot) < -1$ when $BR_1(q_2) = r_1^C(q_2)$ is similar. When $BR_1(q_2) = Q_1 - q_2$, it is obvious that $BR'_1(\cdot) = -1$. Finally, when $BR_1(q_2) = r_1^E(q_2)$, then

$$BR'_{1}(\cdot) = -\frac{\frac{\partial \pi_{1}^{2}(q_{1}^{*}, q_{2}^{*})}{\partial q_{1}^{2}}}{\frac{\partial \pi_{1}^{2}(q_{1}^{*}, q_{2}^{*})}{\partial q_{1}\partial q_{2}}} = -\frac{2p' + p''\left(q_{1} + \gamma\tau Q_{1}\right)}{p' + p''\left(q_{1} + \gamma\tau Q_{1}\right)} < -1,$$

where the inequality is implied by Assumption A1.

Proof of Lemma 2: Suppose that p_1 is excessive and assume by way of negation that $q_1^* = 0$ when firm 2 enters. Then firm 2 produces the monopoly output in period 2, since $r_2^C(0) = Q^M$. For p_1 to be excessive, it must be that $Q_1 < Q^M$. Moreover, given Assumption A2, $\gamma \tau Q_1 < Q_1 \leq Q^M$. Since p_1 is excessive, firm 1's best-response function against q_2 is $r_1^E(q_2)$. Evaluating the second line in (17) at $(0, Q^M)$, and noting that Q^M is defined implicitly by the first-order condition $p(Q^M) + p'(Q^M)Q^M = c,$

$$\frac{\partial \pi_1\left(0,Q^M\right)}{\partial q_1} = p(Q^M) - c + \gamma \tau p'\left(Q^M\right)Q_1 = -p'(Q^M)\left(Q^M - \gamma \tau Q_1\right) > 0$$

where the inequality follows since $p'(\cdot) < 0$ and $Q^M > \gamma \tau Q_1$. Hence, $r_1^E(Q^M) > 0$, contradicting the assumption that $q_1^* = 0$.

Proof of Lemma 4: The monopoly output, Q^M is defined by

$$\pi'(Q_1) = p(Q_1) + p'(Q_1)Q_1 - c = 0$$

Evaluating $\pi'(Q_1)$ at \overline{Q}_1 and using (3),

$$\pi'\left(\overline{Q}\right) = p\left(\overline{Q}_{1}\right) + p'\left(\overline{Q}_{1}\right)\overline{Q}_{1} - c = p'\left(\overline{Q}_{1}\right)\left(\frac{1-\gamma\tau}{2}\right)\overline{Q}_{1} < 0,$$

where the inequality follows by Assumption A2. Hence, $\overline{Q} > Q^M$.

The Cournot equilibrium is defined by $\pi'_1(q_1, q_2) = 0$ and $\pi'_2(q_1, q_2) = 0$, where

$$\pi'_{i}(q_{1}, q_{2}) = p(q_{1} + q_{2}) + p'(q_{1} + q_{2})q_{i} - c.$$

Since the equilibrium is symmetric, $q_1^{\cal C}=q_2^{\cal C}=q^{\cal C},$

$$\pi'_{i}(q_{1}^{C}, q_{2}^{C}) = p(2q^{C}) + p'(2q^{C})q^{C} - c = 0.$$

Evaluating this equation at \overline{Q}_1 and using (3),

$$\pi'_{i}\left(\overline{Q}\right) = p\left(\overline{Q}_{1}\right) + p'\left(\overline{Q}_{1}\right)\frac{\overline{Q}_{1}}{2} - c = -\gamma\tau p'\left(\overline{Q}_{1}\right)\frac{\overline{Q}_{1}}{2} > 0.$$

Hence, $\overline{Q} < q_1^C + q_2^C$.

Next, differentiating equation (3) with respect to \overline{Q}_1 and $\gamma \tau$, and rearranging terms,

$$\frac{\partial \overline{Q}_1}{\partial (\gamma \tau)} = \frac{-\frac{p'(\overline{Q}_1)\overline{Q}_1}{2}}{p'(\overline{Q}_1)\left(1 + \frac{1 + \gamma \tau}{2}\right) + p''(\overline{Q}_1)\left(\frac{1 + \gamma \tau}{2}\right)\overline{Q}_1}.$$

Assumption A1 ensure that the denominator is negative and hence, $\frac{\partial \overline{Q}_1}{\partial (\gamma \tau)} < 0.$

Proof of Lemma 5: First, suppose that $Q_1 < \overline{Q}_1$. Then the Nash equilibrium is defined by the intersection of $r_1^E(q_2)$ and $r_2^C(q_1)$. Fully differentiating this system yields the following comparative statics matrix

$$\frac{2p' + p''(q_1^* + \gamma \tau Q_1)}{p' + p''q_2^*} \left| \begin{array}{c} \times \left| \begin{array}{c} \frac{\partial q_1^*}{\partial Q_1} \\ \frac{\partial q_2^*}{\partial Q_1} \end{array} \right| = \left| \begin{array}{c} -\gamma \tau p' \\ 0 \end{array} \right| \right|$$

where the arguments of p' and p'' are suppressed to ease notation. Hence,

$$\frac{\partial q_1^*}{\partial Q_1} = \frac{-\gamma \tau p' \left(2p' + p'' q_2^*\right)}{\left(2p' + p'' \left(q_1^* + \gamma \tau Q_1\right)\right) \left(2p' + p'' q_2^*\right) - \left(p' + p'' \left(q_1^* + \gamma \tau Q_1\right)\right) \left(p' + p'' q_2^*\right)} \\
= -\frac{\gamma \tau \left(2p' + p'' q_2^*\right)}{3p' + p'' \left(q_1^* + q_2^* + \gamma \tau Q_1\right)},$$

and

$$\frac{\partial q_2^*}{\partial Q_1} = \frac{\gamma \tau p' \left(p' + p'' q_2^*\right)}{\left(2p' + p'' \left(q_1^* + \gamma \tau Q_1\right)\right) \left(2p' + p'' q_2^*\right) - \left(p' + p'' \left(q_1^* + \gamma \tau Q_1\right)\right) \left(p' + p'' q_2^*\right)} \\
= \frac{\gamma \tau \left(p' + p'' q_2^*\right)}{3p' + p'' \left(q_1^* + q_2^* + \gamma \tau Q_1\right)}.$$

Since $\frac{p' + p'' q_2^*}{3p' + p'' \left(q_1^* + q_2^* + \gamma \tau Q_1\right)} = \frac{1}{1 + \frac{2p' + p'' \left(q_1^* + \gamma \tau Q_1\right)}{p' + p'' q_2^*}} < 1$ by Assumption A1, $-\gamma \tau < \frac{\partial q_1^*}{\partial Q_1} < 0 < \frac{\partial q_2^*}{\partial Q_1} < \gamma \tau$.

Moreover, using Assumption A1, it follows that whenever $Q_1 < \overline{Q}_1$,

$$\frac{\partial (q_1^* + q_2^*)}{\partial Q_1} = -\frac{\gamma \tau (2p' + p'' q_2^*)}{3p' + p'' (q_1^* + q_2^* + \gamma \tau Q_1)} + \frac{\gamma \tau (p' + p'' q_2^*)}{3p' + p'' (q_1^* + q_2^* + \gamma \tau Q_1)} \\
= \frac{-p' \gamma \tau}{3p' + p'' (q_1^* + q_2^* + \gamma \tau Q_1)} \in (-\gamma \tau, 0).$$

Now suppose that $Q_1 \ge \overline{Q}_1$. Then the Nash equilibrium is defined by the intersection of $q_1 = Q_1 - q_2$ and $r_2^C(q_1)$. Fully differentiating this system, yields the following comparative statics matrix

$$\begin{vmatrix} 1 & 1 \\ p' + p''q_2^* & 2p' + p''q_2^* \end{vmatrix} \times \begin{vmatrix} \frac{\partial q_1^*}{\partial Q_1} \\ \frac{\partial q_2^*}{\partial Q_1} \end{vmatrix} = \begin{vmatrix} 1 \\ 0 \end{vmatrix},$$

Hence, by Assumption A1,

$$\frac{\partial q_1^*}{\partial Q_1} = \frac{2p' + p''q_2^*}{p'} > 1, \qquad \frac{\partial q_2^*}{\partial Q_1} = -\frac{p' + p''q_2^*}{p'} < 0.$$

It is now easy to see that $\frac{\partial(q_1^*+q_2^*)}{\partial Q_1} = 1.$

Proof of Lemma 7: First, we prove that $Q_1^* > Q^M$. To this end, note that since $\overline{Q}_1 > Q^M$ by Lemma 4, p_1 is excessive when $Q_1 = Q^M$, so $\Pi_1(Q_1)$ is given by the first line of (4). Differentiating the expression and using the envelope theorem (the derivative of the square bracketed term with respect to q_1^* vanishes), yields

$$\Pi_{1}^{\prime}(Q_{1}) = MR(Q_{1}) - c - \delta\alpha \left[\gamma\tau \left(MR(Q_{1}) - p\left(q_{1}^{*} + q_{2}^{*}\right)\right) - p^{\prime}\left(q_{1}^{*} + q_{2}^{*}\right)\left(q_{1}^{*} + \gamma\tau Q_{1}\right)\frac{\partial q_{2}^{*}}{\partial Q_{1}^{-}}\right], \quad (18)$$

where $\frac{\partial q_2^*}{\partial Q_1^-}$ is the derivative of q_2^* with respect to Q_1 when $Q_1 < \overline{Q}_1$. Evaluating $\Pi'_1(Q_1)$ at Q^M and noting that by definition, $MR(Q^M) = c$,

$$\Pi_{1}'\left(Q^{M}\right) = -\delta\alpha \left[\gamma\tau\left(c-p\left(q_{1}^{*}+q_{2}^{*}\right)\right)-p'\left(q_{1}^{*}+q_{2}^{*}\right)\left(q_{1}^{*}+\gamma\tau Q_{1}^{M}\right)\frac{\partial q_{2}^{*}}{\partial Q_{1}^{-}}\right] \\ = -\delta\alpha p'\left(q_{1}^{*}+q_{2}^{*}\right)\left(q_{1}^{*}+\gamma\tau Q_{1}^{M}\right)\left[\gamma\tau-\frac{\partial q_{2}^{*}}{\partial Q_{1}^{-}}\right] > 0,$$

where the second equality follows by substituting for $p(q_1^* + q_2^*) - c$ from (2) and the inequality follows from Lemma 5 which shows that when $Q_1 < \overline{Q}_1$, $\frac{\partial q_2^*}{\partial Q_1^-} < \gamma \tau$. Since $\Pi'_1(Q^M) > 0$, $Q_1^* > Q^M$.

Second, we examine whether firm 1 has an incentive to raise Q_1^* all the way to the point where p_1 is no longer excessive, i.e., above \overline{Q}_1 . To this end, we first evaluate $\Pi'_1(\overline{Q}_1)$ as \overline{Q}_1 approaches \overline{Q}_1 from below. Using $\Pi'_1(\overline{Q}_1^-)$ to denote the derivative of $\Pi_1(Q_1)$ as Q_1 approaches \overline{Q}_1 from below, and recalling that when $Q_1 < \overline{Q}_1$, $\Pi'_1(Q_1)$ is given by (18), we get

$$\begin{aligned} \Pi_{1}^{\prime}\left(\overline{Q_{1}}\right) &= MR\left(\overline{Q}_{1}\right) - c - \delta\alpha \left[\gamma\tau\left(MR(\overline{Q}_{1}) - p\left(q_{1}^{*} + q_{2}^{*}\right)\right) - p^{\prime}\left(q_{1}^{*} + q_{2}^{*}\right)\left(q_{1}^{*} + \gamma\tau\overline{Q}_{1}\right)\frac{\partial q_{2}^{*}}{\partial Q_{1}^{-}}\right] \\ &= MR\left(\overline{Q}_{1}\right) - c - \delta\alpha \left[\gamma\tau\left(MR(\overline{Q}_{1}) - p\left(\overline{Q}_{1}\right)\right) - p^{\prime}\left(\overline{Q}_{1}\right)\left(q_{1}^{*} + \gamma\tau\overline{Q}_{1}\right)\frac{\partial q_{2}^{*}}{\partial Q_{1}^{-}}\right] \end{aligned} \tag{19} \\ &= p^{\prime}\left(\overline{Q}_{1}\right)\left(\frac{1 - \gamma\tau}{2}\right)\overline{Q}_{1} - \delta\alpha \left[\gamma\tau p^{\prime}\left(\overline{Q}_{1}\right)\overline{Q}_{1} - p^{\prime}\left(\overline{Q}_{1}\right)\left(q_{1}^{*} + \gamma\tau\overline{Q}_{1}\right)\frac{\partial q_{2}^{*}}{\partial Q_{1}^{-}}\right] \\ &= p^{\prime}\left(\overline{Q}_{1}\right)\overline{Q}_{1}\left[\frac{1 - \gamma\tau\left(1 + 2\delta\alpha\right)}{2} + \delta\alpha \left(\frac{q_{1}^{*}}{\overline{Q}_{1}} + \gamma\tau\right)\frac{\partial q_{2}^{*}}{\partial Q_{1}^{-}}\right] \\ &= p^{\prime}\left(\overline{Q}_{1}\right)\overline{Q}_{1}\left[\frac{1 - \gamma\tau\left(1 + 2\delta\alpha\right)}{2} + \delta\alpha \left(\frac{1 + \gamma\tau}{2}\right)\frac{\partial q_{2}^{*}}{\partial Q_{1}^{-}}\right] \\ &= -\delta\alpha \left(\frac{1 + \gamma\tau}{2}\right)p^{\prime}\left(\overline{Q}_{1}\right)\overline{Q}_{1}\left[\frac{\gamma\tau\left(1 + 2\delta\alpha\right) - 1}{\delta\alpha\left(1 + \gamma\tau\right)} - \frac{\partial q_{2}^{*}}{\partial Q_{1}^{-}}\right], \end{aligned}$$

where the second equality follows because by definition, $q_1^* + q_2^* = \overline{Q}_1$, and the third equality

follows by using (3). As for the fifth equality, recall that \overline{Q}_1 satisfies both (2) and (1) when $q_i = q_2$. Subtracting the latter from the former, using the fact that $q_1 + q_2 = \overline{Q}_1$, and rearranging yields,

$$p'\left(\overline{Q}_{1}\right)\left[q_{1}^{*}+\gamma\tau\overline{Q}_{1}-q_{2}^{*}\right]=0,\qquad\Rightarrow\qquad2p'\left(\overline{Q}_{1}\right)\overline{Q}_{1}\left[\frac{q_{1}^{*}}{\overline{Q}_{1}}-\frac{1-\gamma\tau}{2}\right]=0.$$
(20)

Hence, $\frac{q_1^*}{\overline{Q}_1} = \frac{1-\gamma\tau}{2}$ when $Q_1 = \overline{Q}_1$. Since $p'(\overline{Q}_1) < 0$, (19) implies that $\Pi'_1(\overline{Q}_1^-)$ has the same sign as $\frac{\gamma\tau(1+2\delta\alpha)-1}{\delta\alpha(1+\gamma\tau)} - \frac{\partial q_2^*}{\partial Q_1^-}$. Note that by Lemma 5, $0 < \frac{\partial q_2^*}{\partial Q_1^-} < \gamma\tau < 1$ and also note that $\frac{\gamma\tau(1+2\delta\alpha)-1}{\delta\alpha(1+\gamma\tau)}$ is increasing with $\delta\alpha$ from $-\infty$ when $\delta\alpha = 0$ to $\frac{3\gamma\tau-1}{1+\gamma\tau}$ when $\delta\alpha = 1$. Hence, $\Pi'_1(\overline{Q}_1^-) \leq 0$ when $\delta\alpha$ is sufficiently small and moreover, $\Pi'_1(\overline{Q}_1^-) \leq 0$ for all $\delta\alpha$ when $\gamma\tau \leq \frac{1}{3}$. In particular, $\delta\alpha \leq \frac{1-\gamma\tau}{2\gamma\tau}$ is sufficient to ensure that $\frac{\gamma\tau(1+2\delta\alpha)-1}{\delta\alpha(1+\gamma\tau)} \leq 0$, in which case, $\Pi'_1(\overline{Q}_1^-) \leq 0$. By continuity then, $\Pi'_1(\overline{Q}_1^-) < 0$ when $\delta\alpha$ does not exceed $\frac{1-\gamma\tau}{2\gamma\tau}$ by too much. By contrast, a necessary condition for $\Pi'_1(\overline{Q}_1^-) > 0$ is $\frac{\gamma\tau(1+2\delta\alpha)-1}{\delta\alpha(1+\gamma\tau)} > 0$, or $\delta\alpha > \frac{1-\gamma\tau}{2\gamma\tau}$.

Next, we evaluate $\Pi'_1(Q_1)$ as Q_1 approaches \overline{Q}_1 from above. Recalling that when $Q_1 \ge \overline{Q}_1$, $\Pi_1(Q_1)$ is given by the second line of (4), we get

$$\Pi_{1}'(Q_{1}) = MR(Q_{1}) - c + \delta\alpha \left[p'(Q_{1}) q_{1}^{*} + (p(Q_{1}) - c) \frac{\partial q_{1}^{*}}{\partial Q_{1}^{+}} \right],$$
(21)

where $\frac{\partial q_1^*}{\partial Q_1^+}$ is the derivative of q_1^* with respect to Q_1 when $Q_1 > \overline{Q}_1$.

Using $\Pi'_1\left(\overline{Q}_1^+\right)$ to denote the derivative of $\Pi_1\left(Q_1\right)$ as Q_1 approaches \overline{Q}_1 from above, using (3), and recalling from (20) that when $Q_1 = \overline{Q}_1, \frac{q_1^*}{\overline{Q}_1} = \frac{1-\gamma\tau}{2}$,

$$\Pi_{1}^{\prime}\left(\overline{Q}_{1}^{+}\right) = MR\left(\overline{Q}_{1}\right) - c + \delta\alpha \left[p^{\prime}\left(\overline{Q}_{1}\right)q_{1}^{*} + \left(p\left(\overline{Q}_{1}\right) - c\right)\frac{\partial q_{1}^{*}}{\partial Q_{1}^{+}}\right]$$

$$= p^{\prime}\left(\overline{Q}_{1}\right)\left(\frac{1 - \gamma\tau}{2}\right)\overline{Q}_{1} + \delta\alpha \left[p^{\prime}\left(\overline{Q}_{1}\right)q_{1}^{*} + \left(p\left(\overline{Q}_{1}\right) - c\right)\frac{\partial q_{1}^{*}}{\partial Q_{1}^{+}}\right]$$

$$= p^{\prime}\left(\overline{Q}_{1}\right)\left(\frac{1 - \gamma\tau}{2}\right)\overline{Q}_{1} + \delta\alpha \left[p^{\prime}\left(\overline{Q}_{1}\right)q_{1}^{*} - p^{\prime}\left(\overline{Q}_{1}\right)\left(\frac{1 + \gamma\tau}{2}\right)\overline{Q}_{1}\frac{\partial q_{1}^{*}}{\partial Q_{1}^{+}}\right]$$

$$= p^{\prime}\left(\overline{Q}_{1}\right)\overline{Q}_{1}\left[\frac{1 - \gamma\tau}{2} + \delta\alpha \left(\frac{q_{1}^{*}}{\overline{Q}_{1}} - \left(\frac{1 + \gamma\tau}{2}\right)\frac{\partial q_{1}^{*}}{\partial Q_{1}^{+}}\right)\right]$$

$$= -\delta\alpha \left(\frac{1 + \gamma\tau}{2}\right)p^{\prime}\left(\overline{Q}_{1}\right)\overline{Q}_{1}\left[\frac{\partial q_{1}^{*}}{\partial Q_{1}^{+}} - \frac{\left(1 + \delta\alpha\right)\left(1 - \gamma\tau\right)}{\delta\alpha\left(1 + \gamma\tau\right)}\right].$$
(22)

Since $p'\left(\overline{Q}_1\right) < 0$, (22) implies that $\Pi'_1\left(\overline{Q}_1^+\right)$ has the same sign as $\frac{\partial q_1^*}{\partial Q_1^+} - \frac{(1+\delta\alpha)(1-\gamma\tau)}{\delta\alpha(1+\gamma\tau)}$. Recall from Lemma 5 that $\frac{\partial q_1^*}{\partial Q_1^+} > 1$. Since $\frac{(1+\delta\alpha)(1-\gamma\tau)}{\delta\alpha(1+\gamma\tau)}$ is decreasing with $\delta\alpha$ from ∞ when $\delta\alpha = 0$ to $\frac{2(1-\gamma\tau)}{1+\gamma\tau} < 2$ when $\delta\alpha = 1$, it follows that $\Pi'_1\left(\overline{Q}_1^+\right) \leq 0$ for $\delta\alpha$ sufficiently small. In particular,

since $\frac{\partial q_1^*}{\partial Q_1^+} > 1$, a necessary condition for $\Pi_1'\left(\overline{Q}_1^+\right) \le 0$ is $\frac{(1+\delta\alpha)(1-\gamma\tau)}{\delta\alpha(1+\gamma\tau)} > 1$, which is equivalent to $\delta\alpha < \frac{1-\gamma\tau}{2\gamma\tau}$. In turn, $\Pi_1'\left(\overline{Q}_1^+\right) \le 0$ implies $Q_1^* \le \overline{Q}_1$.

By contrast, recalling that $\frac{\partial q_1^*}{\partial Q_1^+} > 1$, it follows that $\frac{(1+\delta\alpha)(1-\gamma\tau)}{\delta\alpha(1+\gamma\tau)} < 1$, or $\delta\alpha > \frac{1-\gamma\tau}{2\gamma\tau}$, is sufficient for $\frac{\partial q_1^*}{\partial Q_1^+} > \frac{(1+\delta\alpha)(1-\gamma\tau)}{\delta\alpha(1+\gamma\tau)}$. Then, $\Pi_1'\left(\overline{Q}_1^+\right) > 0$, in which case $Q_1^* > \overline{Q}_1$, provided that in addition, $\Pi_1'\left(\overline{Q}_1^-\right) \ge 0$.

Altogether then, the analysis of $\Pi'_1(\overline{Q}_1^+)$ and $\Pi'_1(\overline{Q}_1^-)$ implies that there are four possible cases that can arise:

(i)
$$\Pi_1'\left(\overline{Q}_1^-\right) < 0 \text{ and } \Pi_1'\left(\overline{Q}_1^+\right) < 0, \text{ so } Q_1^* < \overline{Q}_1, \text{ when}$$

$$\frac{\partial q_1^*}{\partial Q_1^+} < \frac{(1+\delta\alpha)\left(1-\gamma\tau\right)}{\delta\alpha\left(1+\gamma\tau\right)}, \quad \text{ and } \quad \frac{\partial q_2^*}{\partial Q_1^-} > \frac{\gamma\tau\left(1+2\delta\alpha\right)-1}{\delta\alpha\left(1+\gamma\tau\right)}.$$

Both inequalities hold when $\delta \alpha$ is sufficiently small. Moreover, $\delta \alpha < \frac{1-\gamma\tau}{2\gamma\tau}$ is necessary for the first inequality and sufficient for the second.

(ii)
$$\Pi_1'\left(\overline{Q}_1^-\right) \ge 0$$
 and $\Pi_1'\left(\overline{Q}_1^+\right) < 0$, so $Q_1^* = \overline{Q}_1$, when
$$\frac{\partial q_1^*}{\partial Q_1^+} < \frac{(1+\delta\alpha)\left(1-\gamma\tau\right)}{\delta\alpha\left(1+\gamma\tau\right)}, \qquad \text{and} \qquad \frac{\partial q_2^*}{\partial Q_1^-} \le \frac{\gamma\tau\left(1+2\delta\alpha\right)-1}{\delta\alpha\left(1+\gamma\tau\right)}.$$

Both inequalities cannot hold simultaneously however because $\delta \alpha < \frac{1-\gamma\tau}{2\gamma\tau}$ is necessary for the first inequality, but when it holds, $\frac{\gamma\tau(1+2\delta\alpha)-1}{\delta\alpha(1+\gamma\tau)} < 0$, because

$$\gamma \tau \left(1 + 2\delta \alpha\right) - 1 < \gamma \tau \left(1 + 2\left(\frac{1 - \gamma \tau}{2\gamma \tau}\right)\right) - 1 < 0.$$

Since $\frac{\partial q_2^*}{\partial Q_1^-} > 0$, we cannot have $\frac{\partial q_2^*}{\partial Q_1^-} \le \frac{\gamma \tau (1+2\delta \alpha) - 1}{\delta \alpha (1+\gamma \tau)}$.

(iii) $\Pi'_1\left(\overline{Q}_1^-\right) \ge 0$ and $\Pi'_1\left(\overline{Q}_1^+\right) > 0$, so $Q_1^* > \overline{Q}_1$, when

$$\frac{\partial q_1^*}{\partial Q_1^+} \ge \frac{(1+\delta\alpha)\left(1-\gamma\tau\right)}{\delta\alpha\left(1+\gamma\tau\right)}, \quad \text{and} \quad \frac{\partial q_2^*}{\partial Q_1^-} > \frac{\gamma\tau\left(1+2\delta\alpha\right)-1}{\delta\alpha\left(1+\gamma\tau\right)}.$$

 $\delta \alpha > \frac{1-\gamma \tau}{2\gamma \tau}$ is sufficient for the first inequality and necessary for the second. (iv) $\Pi'_1\left(\overline{Q}_1^-\right) < 0$ and $\Pi'_1\left(\overline{Q}_1^+\right) > 0$, in which case there are two local optima, one below and one above \overline{Q}_1 . This case arises when

$$\frac{\partial q_1^*}{\partial Q_1^+} > \frac{\left(1 + \delta \alpha\right) \left(1 - \gamma \tau\right)}{\delta \alpha \left(1 + \gamma \tau\right)}, \qquad \text{and} \qquad \frac{\partial q_2^*}{\partial Q_1^-} < \frac{\gamma \tau \left(1 + 2\delta \alpha\right) - 1}{\delta \alpha \left(1 + \gamma \tau\right)}.$$

 $\delta \alpha > \frac{1-\gamma \tau}{2\gamma \tau}$ is sufficient for both inequalities.

Proof of Proposition 2: Suppose that $Q_1^* < \overline{Q}_1$. Then Q_1^* is implicitly defined by $\Pi'_1(Q_1) = 0$, where $\Pi'_1(Q_1)$ is given by (18). Fully differentiating the equation, using Assumption A3, and the fact that $\Pi'_1(Q_1) = 0$,

$$\frac{\partial Q_1^*}{\partial (\delta \alpha)} = \frac{\gamma \tau \left(MR(Q_1) - p \left(q_1^* + q_2^*\right)\right) - p' \left(q_1^* + q_2^*\right) \left(q_1^* + \gamma \tau Q_1\right) \frac{\partial q_2^*}{\partial Q_1}}{\Pi_1''(Q_1)} = \frac{MR(Q_1) - c}{\delta \alpha \Pi_1''(Q_1)} > 0,$$

where the inequality follows because $\Pi_{1}^{\prime\prime}(Q_{1}) < 0$ and because $Q_{1}^{*} > Q^{M}$ implies that $MR(Q_{1}) < c$.

Likewise, when $Q_1^* > \overline{Q}_1$, Q_1^* is implicitly defined by $\Pi'_1(Q_1) = 0$, where $\Pi'_1(Q_1)$ is given by (21). Fully differentiating the equation, using Assumption A3, and the fact that $\Pi'_1(Q_1) = 0$,

$$\frac{\partial Q_1^*}{\partial (\delta \alpha)} = -\frac{p'(Q_1) q_1^* + (p(Q_1) - c) \frac{\partial q_1^*}{\partial Q_1^+}}{\Pi_1''(Q_1)} = \frac{MR(Q_1) - c}{\delta \alpha \Pi_1''(Q_1)} > 0$$

where the inequality follows because $\Pi_1''(Q_1) < 0$ and because $Q_1^* > Q^M$ implies that $MR(Q_1) < c$.

As for $\gamma \tau$, note that when $Q_1^* > \overline{Q}_1$, $\Pi_1(Q_1)$ is independent of $\gamma \tau$.

Proof of Lemma 8: The best-response function of firm 2 is defined by the familiar Cournot best-response function,

$$BR_2(q_1) = r_2^C(q_1) = \frac{A - q_1}{2}.$$

The best-response function of firm 1 is equal to the Cournot best-response function $r_1^C(q_2) = \frac{A-q_2}{2}$ if $q_1 + q_2 \leq Q_1$, i.e., if $\frac{A-q_2}{2} + q_2 = \frac{A+q_2}{2} \leq Q_1$. If $q_1 + q_2 > Q_1$, p_1 is deemed excessive with probability γ , so the best-response function of firm 1 maximizes the second line of $\pi_1(q_1, q_2)$ and hence is given by $r_1^E(q_2) = \frac{A-q_2}{2} - \frac{\gamma\tau Q_1}{2}$. But then $r_1^E(q_2) + q_2 \geq Q_1$ only if $\frac{A-q_2}{2} - \frac{\gamma\tau Q_1}{2} + q_2 > Q_1$, or $\frac{A+q_2}{2+\gamma\tau Q_1} > Q_1$. And if $\frac{A+q_2}{2+\gamma\tau Q_1} \leq Q_1 < \frac{A+q_2}{2}$, the best-response function of firm 1 is $Q_1 - q_2$. Using the definitions of $r_1^C(q_2)$ and $r_1^E(q_2)$, and rearranging terms, we have:

$$BR_1(q_2) = \begin{cases} r_1^C(q_2) = \frac{A-q_2}{2}, & \frac{A+q_2}{2} \le Q_1, \\ Q_1 - q_2, & \frac{A+q_2}{2+\gamma\tau Q_1} \le Q_1 < \frac{A+q_2}{2}, \\ r_1^E(q_2) = \frac{A-q_2}{2} - \frac{\gamma\tau Q_1}{2}, & Q_1 < \frac{A+q_2}{2+\gamma\tau Q_1}. \end{cases}$$

It can be easily checked that this expression coincides with the best-response function of firm 1 characterized in Lemma 1 when p = a - Q.

The Nash equilibrium in period 2 is attained at the intersection of $BR_1(q_2)$ and $BR_2(q_1)$. There are three possible cases to consider. First, if the Cournot best-response functions, $r_1^C(q_2)$ and $r_2^C(q_1)$, intersect below the $q_1+q_2 = Q_1$ line, we obtain the Cournot equilibrium, $(q_1^C, q_2^C) = (\frac{A}{3}, \frac{A}{3})$. This equilibrium can arise however only if the aggregate output, $\frac{2A}{3}$, is below Q_1 . But if $\frac{2A}{3} < Q_1$, firm 1 can lower Q_1 towards the monopoly output $\frac{A}{2}$ and thereby raise its period 1 profit without making p_1 excessive (since $Q_1 > \frac{2A}{3}$). Hence in equilibrium, $Q_1 \leq \frac{2A}{3}$, meaning that the Cournot outcome is not an equilibrium in our model.

Second, suppose that $r_1^E(q_2)$ and $r_2^C(q_1)$ intersect above the $q_1 + q_2 = Q_1$ line. Then the equilibrium is given by $\left(\frac{A-2\gamma\tau Q_1}{3}, \frac{A+\gamma\tau Q_1}{3}\right)$. This case can arise, however, only if the aggregate output in equilibrium, $\frac{2A-\gamma\tau Q_1}{3}$, exceeds Q_1 , or equivalently if $Q_1 < \frac{2A}{3+\gamma\tau} \equiv \overline{Q}_1$. Notice that since $\gamma\tau \leq 1$, $Q_1 < \frac{A}{2\gamma\tau}$, which implies in turn that $q_1^* = \frac{A-2\gamma\tau Q_1}{3} > 0$. Moreover, note that as Lemma 4 shows, $\overline{Q}_1 > \frac{A}{2} \equiv Q^M$.

Third, if $\frac{2A}{3+\gamma\tau} \leq Q_1 < \frac{2A}{3}$, the equilibrium is attained at the intersection of $r_2^C(q_1) = \frac{A-q_1}{2}$ and $q_1 = Q_1 - q_2$, and is given by $(2Q_1 - A, A - Q_1)$.

Proof of Proposition 3: Note that $\Pi_1(Q_1)$ is continuous at $Q_1 = \frac{2A}{3+\gamma\tau} \equiv \overline{Q}_1$. Differentiating $\Pi_1(Q_1)$ yields,

$$\Pi_{1}'(Q_{1}) = \begin{cases} A - 2Q_{1} - \frac{\delta\alpha\gamma\tau}{9} \left[7A - 2\left(9 + \gamma\tau\right)Q_{1}\right], & Q_{1} < \frac{2A}{3+\gamma\tau}, \\ A - 2Q_{1} + \delta\alpha\left(3A - 4Q_{1}\right), & \frac{2A}{3+\gamma\tau} \le Q_{1} \le \frac{2A}{3}. \end{cases}$$
(23)

Note that $\Pi_1''(Q_1) < 0$ for $\frac{2A}{3+\gamma\tau} \leq Q_1 \leq \frac{2A}{3}$ and $\Pi_1''(Q_1) \leq 0$ for $Q_1 < \frac{2A}{3+\gamma\tau}$, provided that $\delta \alpha \leq \frac{9}{\gamma\tau(9+\gamma\tau)}$, where $\frac{9}{\gamma\tau(9+\gamma\tau)} > 0.9$ since $\gamma\tau < 1$ by Assumption A2. Consequently, $\delta \alpha \leq 0.9$ is sufficient to ensure that $\delta \alpha \leq \frac{9}{\gamma\tau(9+\gamma\tau)}$, in which case $\Pi_1(Q_1)$ is piecewise concave.

Evaluating $\Pi'_1(Q_1)$ as Q_1 approaches $\overline{Q}_1 \equiv \frac{2A}{3+\gamma\tau}$ from below and noting that in this case,

 $\Pi'_1(Q_1)$ is given by the first line in (23) yields,

$$\begin{aligned} \Pi_{1}^{\prime}\left(\overline{Q_{1}}\right) &= A - \frac{4A}{3 + \gamma\tau} - \frac{\delta\alpha\gamma\tau}{9} \left[7A - \frac{4A\left(9 + \gamma\tau\right)}{3 + \gamma\tau}\right] \\ &= \frac{A}{9\left(3 + \gamma\tau\right)} \left[27 + 9\gamma\tau - 36 - 7\delta\alpha\gamma\tau\left(3 + \gamma\tau\right) + 4\delta\alpha\gamma\tau\left(9 + \gamma\tau\right)\right] \\ &= \frac{3A\gamma\tau\left(5 - \gamma\tau\right)}{9\left(3 + \gamma\tau\right)} \left[\delta\alpha - \frac{3\left(1 - \gamma\tau\right)}{\gamma\tau\left(5 - \gamma\tau\right)}\right]. \end{aligned}$$

Likewise, evaluating $\Pi'_1(Q_1)$ when Q_1 approaches $\overline{Q}_1 \equiv \frac{2A}{3+\gamma\tau}$ from above and noting that in this case $\Pi'_1(Q_1)$ is given by the second line in (23),

$$\Pi_{1}'\left(\overline{Q}_{1}^{+}\right) = A - \frac{4A}{3 + \gamma\tau} + \delta\alpha \left(3A - \frac{8A}{3 + \gamma\tau}\right)$$
$$= \frac{A}{3 + \gamma\tau} \left[3 + \gamma\tau - 4 + 9\delta\alpha + 3\delta\alpha\gamma\tau - 8\delta\alpha\right]$$
$$= \frac{A\left(1 + 3\gamma\tau\right)}{3 + \gamma\tau} \left[\delta\alpha - \frac{1 - \gamma\tau}{1 + 3\gamma\tau}\right].$$

Noting that

$$\frac{3\left(1-\gamma\tau\right)}{\gamma\tau\left(5-\gamma\tau\right)} - \frac{1-\gamma\tau}{1+3\gamma\tau} = \frac{\left(1-\gamma\tau\right)\left(3+4\gamma\tau+\left(\gamma\tau\right)^{2}\right)}{\gamma\tau\left(5-\gamma\tau\right)\left(1+3\gamma\tau\right)} > 0,$$

there are now three cases to consider:

(i) If
$$\delta \alpha < \frac{1-\gamma\tau}{1+3\gamma\tau} < \frac{3(1-\gamma\tau)}{\gamma\tau(5-\gamma\tau)}$$
, then $\Pi'_1(\overline{Q}_1) < 0$ and $\Pi'_1(\overline{Q}_1^+) < 0$, so $Q_1^* < \overline{Q}_1$. Then,

 $\Pi'_1(Q_1)$ is given by the first line in (23). Setting it equal to 0 and solving yields the expression in the first line of (6). Note that

$$\frac{2A}{3+\gamma\tau} - \frac{A}{2} \left[\frac{9 - 7\delta\alpha\gamma\tau}{9 - \delta\alpha\gamma\tau \left(9 + \gamma\tau\right)} \right] = \frac{3A\gamma\tau \left(5 - \gamma\tau\right) \left[\frac{3(1-\gamma\tau)}{\gamma\tau(5-\gamma\tau)} - \delta\alpha \right]}{2\left(3 + \gamma\tau\right) \left(9 - \delta\alpha\gamma\tau \left(9 + \gamma\tau\right)\right)}$$

Hence, $\frac{A}{2} \begin{bmatrix} \frac{9-7\delta\alpha\gamma\tau}{9-\delta\alpha\gamma\tau(9+\gamma\tau)} \end{bmatrix} < \overline{Q}_1 \equiv \frac{2A}{3+\gamma\tau}$ whenever $\delta\alpha < \frac{3(1-\gamma\tau)}{\gamma\tau(5-\gamma\tau)}$ (otherwise, $Q_1^* = \overline{Q}_1$). (ii) If $\delta\alpha > \frac{3(1-\gamma\tau)}{\gamma\tau(5-\gamma\tau)} > \frac{1-\gamma\tau}{1+3\gamma\tau}$, then $\Pi_1'(\overline{Q}_1^-) > 0$ and $\Pi_1'(\overline{Q}_1^+) > 0$, so $Q_1^* > \overline{Q}_1$. Now $\Pi_1'(Q_1)$ is given by the second line in (23); setting it equal to 0 and solving yields the expression

 $\Pi'_1(Q_1)$ is given by the second line in (23); setting it equal to 0 and solving yields the expression in the second line of (6). Note that

$$\frac{A}{2}\left[\frac{1+3\delta\alpha}{1+2\delta\alpha}\right] - \frac{2A}{3+\gamma\tau} = \frac{A\left(1+3\gamma\tau\right)\left[\delta\alpha - \frac{1-\gamma\tau}{1+3\gamma\tau}\right]}{2\left(1+2\delta\alpha\right)\left(3+\gamma\tau\right)}.$$

Hence, $\delta \alpha \geq \frac{1-\gamma\tau}{1+3\gamma\tau}$ ensures that $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right] \geq \overline{Q}_1 \equiv \frac{2A}{3+\gamma\tau}$ (when $\delta \alpha < \frac{1-\gamma\tau}{1+3\gamma\tau}$, $Q_1^* = \overline{Q}_1$). (iii) If $\frac{1-\gamma\tau}{1+3\gamma\tau} \leq \delta \alpha < \frac{3(1-\gamma\tau)}{\gamma\tau(5-\gamma\tau)}$, then $\Pi_1'(\overline{Q}_1^-) < 0 \leq \Pi_1'(\overline{Q}_1^+)$, so both $\frac{A}{2} \left[\frac{9-7\delta\alpha\gamma\tau}{9-\delta\alpha\gamma\tau(9+\gamma\tau)} \right]$ and $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ are local maxima. To determine which is a global maximum, note that when $\delta \alpha$ is close to $\frac{1-\gamma\tau}{1+3\gamma\tau}$, $\Pi_1'(\overline{Q}_1^+)$ goes to 0, while $\Pi_1'(\overline{Q}_1^-) < 0$. Hence, $\frac{A}{2} \left[\frac{9-7\delta\alpha\gamma\tau}{9-\delta\alpha\gamma\tau(9+\gamma\tau)} \right]$ is a global maximum. By contrast, when $\delta \alpha$ goes to $\frac{3(1-\gamma\tau)}{\gamma\tau(5-\gamma\tau)}$, $\Pi_1'(\overline{Q}_1^-)$ goes to 0, while $\Pi_1'(\overline{Q}_1^+) > 0$, so $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum. Substituting $Q_1 = \frac{A}{2} \left[\frac{9-7\delta\alpha\gamma\tau}{9-\delta\alpha\gamma\tau(9+\gamma\tau)} \right]$ into the first line of (5) and $Q_1 = \frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ into the second line of (5) and comparing the resulting expressions, reveals that $\frac{A}{2} \left[\frac{9-7\delta\alpha\gamma\tau}{9-\delta\alpha\gamma\tau(9+\gamma\tau)} \right]$ is a global maximum if $\delta \alpha < Z(\gamma\tau)$, whereas $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum if $\delta \alpha > Z(\gamma\tau)$, whereas $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum if $\delta \alpha > Z(\gamma\tau)$, whereas $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum if $\delta \alpha > Z(\gamma\tau)$, whereas $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum if $\delta \alpha > Z(\gamma\tau)$, whereas $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum if $\delta \alpha > Z(\gamma\tau)$, whereas $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum if $\delta \alpha > Z(\gamma\tau)$, whereas $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum if $\delta \alpha > Z(\gamma\tau)$, whereas $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum if $\delta \alpha > Z(\gamma\tau)$, whereas $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum if $\delta \alpha > Z(\gamma\tau)$, whereal $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum if $\delta \alpha > Z(\gamma\tau)$, whereal $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum if $\delta \alpha > Z(\gamma\tau)$, whereal $\frac{A}{2} \left[\frac{1+3\delta\alpha}{1+2\delta\alpha} \right]$ is a global maximum if $\delta \alpha > Z(\gamma\tau)$.

The equilibrium values in period 2 are obtained by substituting Q_1^* into the period 2 equilibrium, which is $\left(\frac{A-2\gamma\tau Q_1}{3}, \frac{A+\gamma\tau Q_1}{3}\right)$ if $Q_1 < \frac{2A}{3+\gamma\tau}$ and $(2Q_1 - A, A - Q_1)$ if $\frac{2A}{3+\gamma\tau} \leq Q_1 < \frac{2A}{3}$.

Proof of Proposition 4: Note from (9) that $CS(Q_1^*)$ depends on $\gamma\tau$ only through Q_1^* . But when $\delta \alpha \geq Z(\gamma\tau)$, (6) shows that Q_1^* is independent of $\gamma\tau$, so $\frac{\partial CS(Q_1^*)}{\partial(\gamma\tau)} = 0$. Next suppose that $\delta \alpha < Z(\gamma\tau)$. Then,

$$\frac{\partial CS\left(Q_{1}^{*}\right)}{\partial\left(\gamma\tau\right)} = \left[Q_{1}^{*} - \delta\alpha\left(\frac{2A - \gamma\tau Q_{1}^{*}}{3}\right)\frac{\gamma\tau}{3}\right]\frac{\partial Q_{1}^{*}}{\partial\left(\gamma\tau\right)} \\ = \frac{1}{9}\left[\left(9 + \delta\alpha\left(\gamma\tau\right)^{2}\right)Q_{1}^{*} - 2\delta\alpha\gamma\tau A\right]\frac{\partial Q_{1}^{*}}{\partial\left(\gamma\tau\right)},$$

where $\frac{\partial Q_1^*}{\partial (\gamma \tau)} > 0$. Using (6), the square bracketed expression is given by

$$\begin{pmatrix} 9+\delta\alpha (\gamma\tau)^2 \end{pmatrix} \frac{A}{2} \left[\frac{9-7\delta\alpha\gamma\tau}{9-\delta\alpha\gamma\tau (9+\gamma\tau)} \right] - 2\delta\alpha\gamma\tau A = \frac{A \left[(9-7\delta\alpha\gamma\tau) \left(9+\delta\alpha (\gamma\tau)^2 \right) - 4\delta\alpha\gamma\tau (9-\delta\alpha\gamma\tau (9+\gamma\tau)) \right]}{2 \left(9-\delta\alpha\gamma\tau (9+\gamma\tau) \right)},$$

which is positive for all $\delta \alpha < 0.9$ (this is verified with Mathematica), and hence for all $\delta \alpha < Z(\gamma \tau)$.²⁶ Hence, $\frac{\partial CS(Q_1^*)}{\partial(\gamma \tau)} > 0$.

Proof of Proposition 6: Recall that $\underline{p}(p_1)$ is defined implicitly by $Q(\underline{p}(p_1))(\underline{p}(p_1)-c) =$

²⁶The expression depends on two parameters: $\delta \alpha$ and $\gamma \tau$. A three dimensional plot shows that the expression is positive for all $\delta \alpha < 0.9$.

 $\gamma \tau \left(p_1 - \underline{p} \left(p_1 \right) \right) Q \left(p_1 \right)$. Then, the first-order condition for p_1 is given by

$$\Pi'(p_{1}) = Q(p_{1}) + Q'(p_{1})(p_{1} - c)$$

$$-\delta\alpha \left[Q(\underline{p}(p_{1}))(\underline{p}(p_{1}) - c) - \gamma\tau Q(p_{1})(p_{1} - \underline{p}(p_{1}))\right] f(\underline{p}(p_{1}))\underline{p}'(p_{1})$$

$$-\delta\alpha\gamma\tau \int_{\underline{p}(p_{1})}^{p_{1}} \left[Q(p_{1}) + Q'(p_{1})(p_{1} - c_{2})\right] dF(c_{2})$$

$$= Q(p_{1}) + Q'(p_{1})(p_{1} - c) - \delta\alpha\gamma\tau \int_{\underline{p}(p_{1})}^{p_{1}} \left[Q(p_{1}) + Q'(p_{1})(p_{1} - c_{2})\right] dF(c_{2}) = 0$$

Consistent with Proposition 2, the first-order condition implies that p_1 is decreasing with $\delta \alpha$, which is the discounted probability that firm 2 is born.

Evaluating $\Pi'(p_1)$ at p^M and recalling that p^M is implicitly defined by $Q(p^M) + Q'(p^M)(p^M - c) = 0$, yields

$$\Pi'(p^{M}) = -\delta\alpha\gamma\tau \int_{\underline{p}(p^{M})}^{p^{M}} \left[Q(p^{M}) + Q'(p^{M})(p^{M} - c_{2})\right] dF(c_{2})$$
$$= \delta\alpha\gamma\tau Q'(p^{M}) \int_{\underline{p}(p^{M})}^{p^{M}} (c_{2} - c) dF(c_{2}) < 0.$$

Hence, the prohibition of excessive pricing induces firm 1 to lower p_1 below p^M and therefore benefits consumers in period 1.

Proof of Proposition 7: Suppose first that $p_1 > p_{12}$ which is equivalent to $Q_1 < q_1 + bq_2$. Then, the Nash equilibrium is defined by the following first-order conditions:

$$\frac{\partial \Pi_1 \left(Q_1, q_1, q_2 \right)}{\partial Q_1} = A - 2Q_1 - \gamma \tau \left[q_1 + bq_2 - Q_1 \right] + \gamma \tau Q_1 = 0,$$
$$\frac{\partial \Pi_1 \left(Q_1, q_1, q_2 \right)}{\partial q_1} = A - 2q_1 - bq_2 - \gamma \tau Q_1 = 0,$$

and

$$\frac{\partial \Pi_2 (, q_1, q_2)}{\partial q_2} = A - 2q_2 - bq_1 = 0$$

Solving the three equations yields (14)-(15). Straightforward computations reveal that $Q_1^* < q_1^* + bq_2^*$, i.e., p_1 is excessive, if and only if $\gamma \tau < \frac{b(2-b)}{4+b-2b^2}$. Moreover, substituting (14)-(15) into (13) and differentiating with respect to $\gamma \tau$ reveals that p_1 is decreasing with $\gamma \tau$ while p_{21} and p_{22} are increasing with $\gamma \tau$.

Suppose then that $\gamma \tau \geq \frac{b(2-b)}{4+b-2b^2}$, so p_{12} is not excessive. Then, firm 1's profit is given by the top line of $\Pi_1(Q_1, q_1, q_2)$, and in equilibrium, $Q_1^* = \frac{A}{2}$, $q_1^* = q_2^* = \frac{A}{2+b}$. But then $p_1 = \frac{A}{2+b} < \frac{A}{2}$, so p_1 is in fact excessive, a contradiction. Hence, to ensure that p_1 is not excessive, firm 1 must set Q_1 and q_1 such that $Q_1 = q_1 + bq_2$. Its profit then becomes

$$\Pi_1 \left(Q_1, q_1, q_2 \right) = \left(A - q_1 - bq_2 \right) \left(q_1 + bq_2 \right) + \left(A - q_1 - bq_2 \right) q_1.$$

The resulting Nash equilibrium is therefore defined by the following first-order conditions:

$$\frac{\partial \Pi_1 \left(Q_1, q_1, q_2 \right)}{\partial Q_1} = 2A - 4q_1 - 3bq_2 = 0,$$

and

$$\frac{\partial \Pi_2\left(,q_1,q_2\right)}{\partial q_2} = A - 2q_2 - bq_1 = 0.$$

Solving, and using the fact that $Q_1 = q_1 + bq_2$, yields (16).

The equilibrium in the contemporaneous benchmark case under price competition: Repeating the same steps as in Proposition 7, the Nash equilibrium when firms set prices is given by

$$p_{1}^{*} = \frac{A\left(\left(2-b^{2}\right)H - \left(2-b\right)\gamma\tau + b^{2}\left(1+\left(\gamma\tau\right)^{2}\right)\right)}{2\left(\left(1-b^{2}\right)H + \left(2+b^{2}\right)\left(1-\gamma\tau\right)\right)},$$

$$p_{12}^{*} = \frac{A\left(1-b\right)\left(1-\gamma\tau\right)\left(2+\gamma\tau+b\left(1+\gamma\tau\right)\right)}{\left(1-b^{2}\right)H + \left(2+b^{2}\right)\left(1-\gamma\tau\right)}, \qquad p_{22}^{*} = \frac{A\left(1-b\right)\left(\left(1+b\right)H + 2\left(1-\gamma\tau\right) + b\gamma\tau\left(1+b\right)\right)}{2\left(\left(1-b^{2}\right)H + \left(2+b^{2}\right)\left(1-\gamma\tau\right)\right)},$$
if $\gamma\tau < \frac{b(2+b)}{4+b-2b^{2}}$ and by
$$p_{1}^{*} = p_{12}^{*} = \frac{A\left(1-b\right)\left(4+3b\right)}{8-5b^{2}}, \qquad p_{22}^{*} = \frac{A\left(1-b\right)\left(4+3b-b\left(1+b\right)\right)}{8-5b^{2}}.$$

if
$$\gamma \tau \geq \frac{b(2+b)}{4+b-2b^2}$$
. When $\gamma \tau < \frac{b(2+b)}{4+b-2b^2}$, p_1 exceeds p_{12} , in which case p_1 is excessive. Differentiating the equilibrium prices with respect to $\gamma \tau$, reveals that an increase in $\gamma \tau$ leads to a decrease in p_1

and an increase in p_{12} and p_{22} .

7 References

Areeda P. and H. Hovenkamp (2001), Antitrust Law, Aspen Publishers, 2nd Ed.

- Baumol W. (1979) "Quasi-Permanence of Price Reductions: A Policy for Prevention of Predatory Pricing," Yale Law Journal, 89, 1-26.
- Besanko, D., and T. Lyon (1993), "Equilibrium Incentives for Most-Favored Customer Clauses in an Oligopolistic Industry," International Journal of Industrial Organization, 11, 347–367.
- Cooper, T. E. (1986), "Most-Favored-Customer Pricing and Tacit Collusion," RAND Journal of Economics, 17, 377-388.
- Deneckere, R. and D. Kovenock (1996) "Bertrand-Edgeworth Duopoly with Unit Cost Asymmetry," *Economic Theory*, 8, 1-25.
- Economic Advisory Group on Competition Policy (2005), "An Economic Approach to Article 82," Report for the DG Competition.
- Edlin A. (2002), "Stopping Above-Cost Predatory Pricing," Yale Law Journal, 111, 941-991.
- Edlin A., C. Roux, A. Schmutzlerk, and C. Thöni (2016), "Hunting Unicorns? Experimental Evidence on Predatory Pricing Policies," University of Zurich, Department of Economics, Working Paper No. 258
- Evans D. and J. Padilla (2005), "Excessive Prices: Using Economics to Define Administrable Legal Rules," Journal of Competition Law and Economics, 1(1): 97-122.
- Ezrachi, A. and D. Gilo (2009) "Are Excessive Prices Really Self-Correcting?," Journal of Competition Law and Economics, 5, 249-268.
- Ezrachi, A. and D. Gilo (2010a) "The Darker Side of the Moon–The Assessment of Excessive Pricing and Proposal for a Post-entry Price-cut Benchmark" in Studies of the Oxford Institute of European and Comparative Law, Hart publishing.
- Ezrachi, A. and D. Gilo (2010b), "Excessive Pricing, Entry, Assessment, and Investment: Lessons From The Mittal Litigation," Antitrust Law Journal, 76, p. 873.
- Gal M. (2004) "Monopoly Pricing as an Antitrust Offense in The U.S. and The EC: Two Systems of Belief about Monopoly?" Antitrust Bulletin, 49, 343-385.

- Gal M. and H. Nevo (2015), "The Influence of Decision Theory on the Design of Legal Rules: Unfair Price as an Abuse of Monopolistic Power," *Mishpatim*, 45, 277-331 (In Hebrew).
- Gal M. and H. Nevo (2016), "High Prices as Abuse: Trojan Horse," forthcoming in *Mishpatim* (In Hebrew).
- Gilo D. (2018) "A Coherent Approach to the Antitrust Prohibition of Excessive Pricing by Dominant Firms," forthcoming in *Excessive Pricing and Competition Law Enforcement*, Jenny F. and Katsoulacos Y. eds., Springer.
- Green N. (2006) "Problems in the Identification of Excessive Prices: The United Kingdom Experience in the Light of NAPP," in European Competition Law Annual 2003: What is an Abuse of a Dominant Position? Ehlermann C.D and I. Atanasiu, eds., Oxford and Portland, Oregon, Hart Publishing.
- Jenny F. (2016), "Abuse of Dominance by Firms Charging Excessive or Unfair Prices: An Assessment," Available at http://www.antitrust.gov.il/files/34246/Excessive%20prices%20Final%20%20Signed%20
- Motta M. and A. de Streel (2006), "Excessive Pricing and Price Squeeze under EU Law," in Claus-Dieter Ehlermann and Isabela Atanasiu (eds.), What is an abuse of a dominant position? Oxford: Hart Publishing.
- Motta M. and A. de Streel (2007), "Excessive Pricing in Competition Law: Never say Never?" in Swedish Competition Authority (eds.), The Pros and Cons of High Prices.
- Neilson W. and H. Winter (1993), "Bilateral Most-Favored-Customer Pricing and Collusion," RAND Journal of Economics, 24(1), 147-155.
- O'Donoghue R. and J.A. Padilla (2006), *The Law and Economics of Article 82 EC*, Oxford: Hart Publishing.
- OECD (2011), "Excessive Prices, Background Paper by the Secretariat," OECD Policy Roundtables, DAF/COMP(2011)18, available at http://www.oecd.org/competition/abuse/49604207.pdf.
- OFT (2004), "Assessment of Conduct: Draft Competition Law Guideline for Consultation," OFT414a, available at http://webarchive.nationalarchives.gov.uk/20131101172401/http://oft.gov.uk/shared
- Schnitzer, M. (1994), "Dynamic Duopoly with Best-Price Clauses," *RAND Journal of Economics*, 25, 186-196.

- Spiegel Y. (2018), "Antitrust Enforcement of the Prohibition of Excessive Prices the Israeli Experience," forthcoming in *Excessive Pricing and Competition Law Enforcement*, Jenny F. and Katsoulacos Y. eds., Springer.
- Williamson O.E. (1977), "Predatory Pricing: A Strategic and Welfare Analysis," Yale Law Journal, 87, 284-340.
- Whish R. (2003), Competition Law, Lexisnexis, 5th Ed.